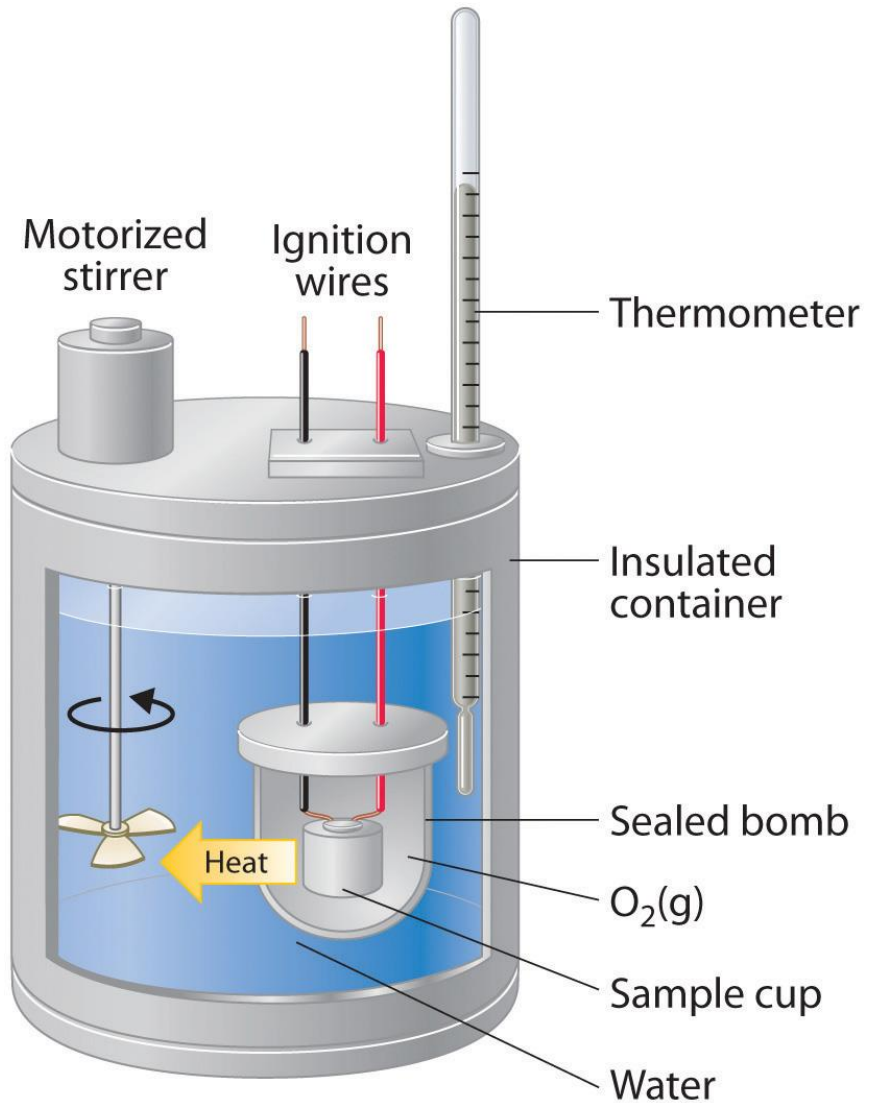
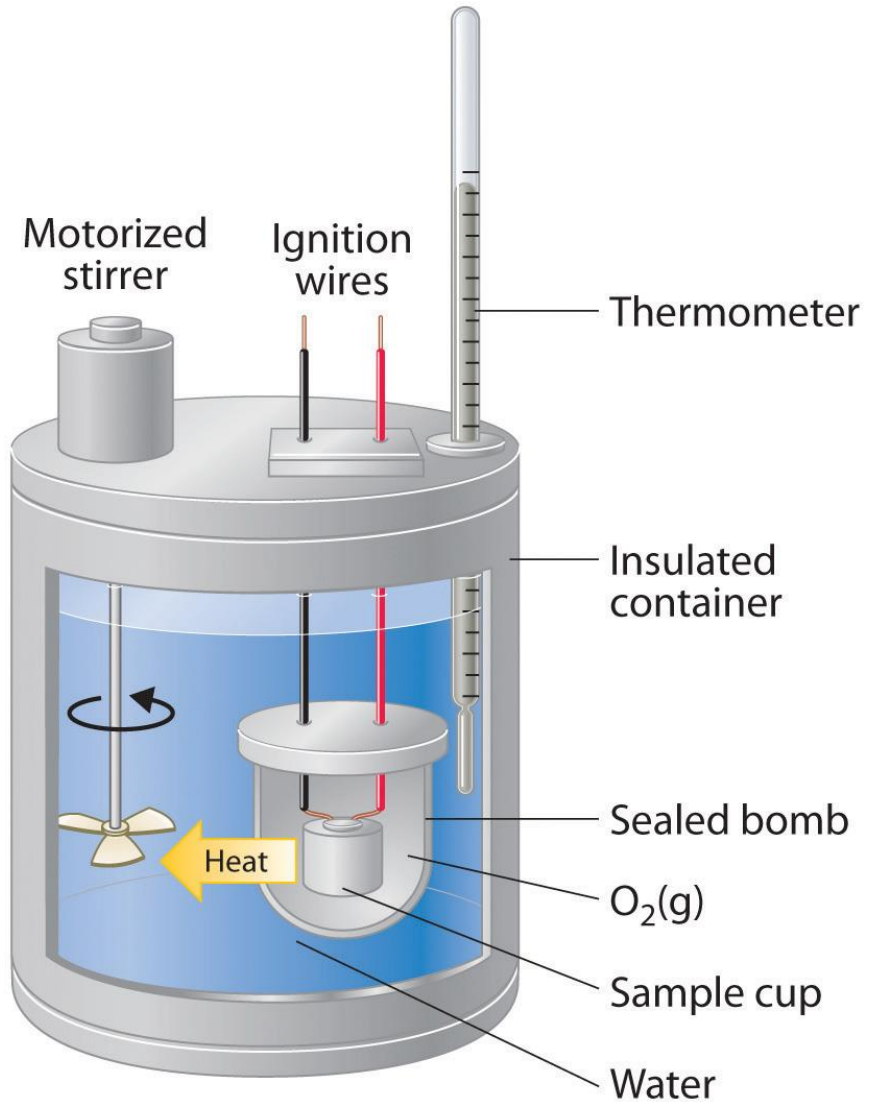


Calorimetry



A constant-volume bomb calorimeter.

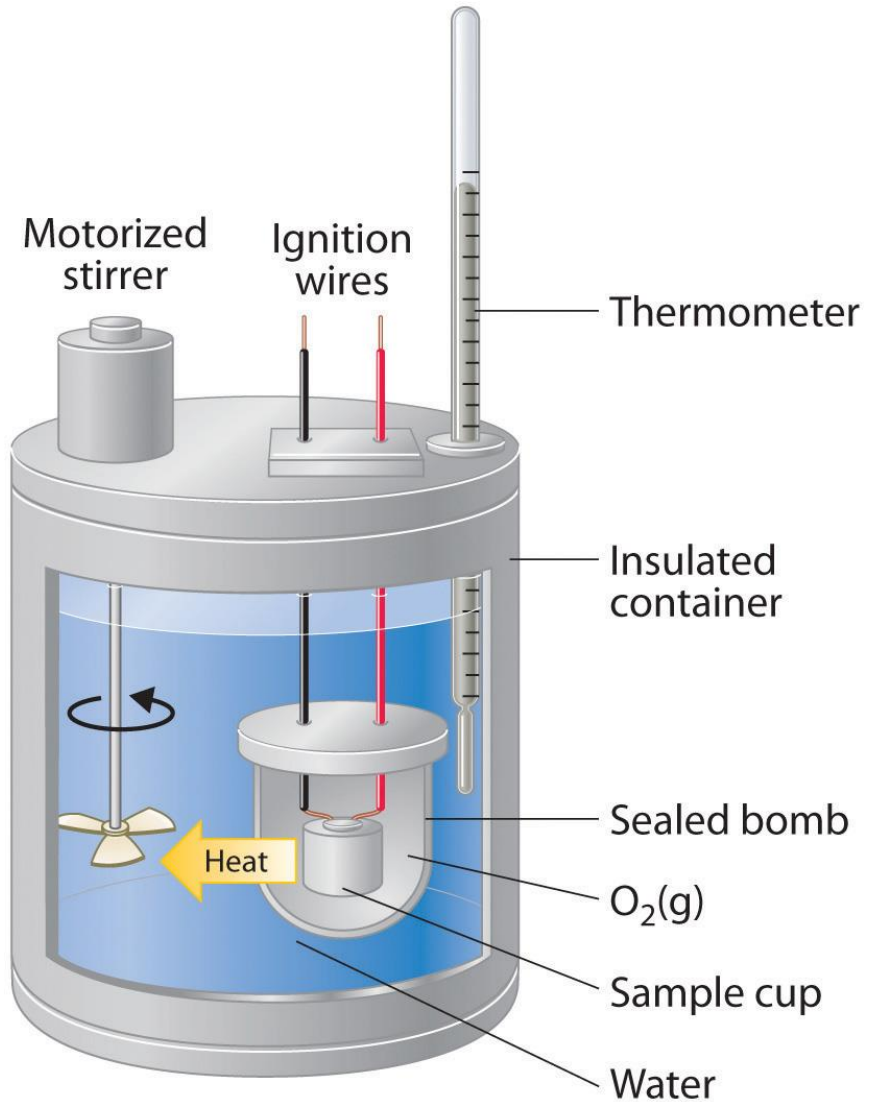
Calorimetry



$$q = C\Delta T$$

A constant-volume bomb calorimeter.

Calorimetry



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↓

calorimeter constant

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Calorimeter constant

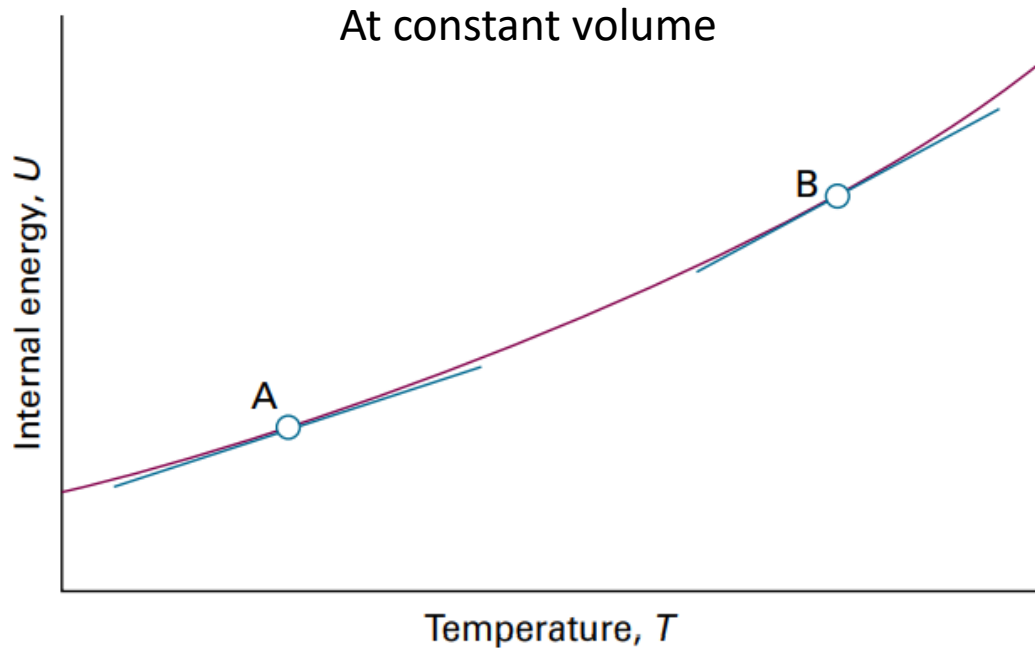
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If the observed rise in temperature is 5.5 K, then the calorimeter constant is $C = (36 \text{ kJ}) / (5.5 \text{ K}) = 6.5 \text{ kJ K}^{-1}$.

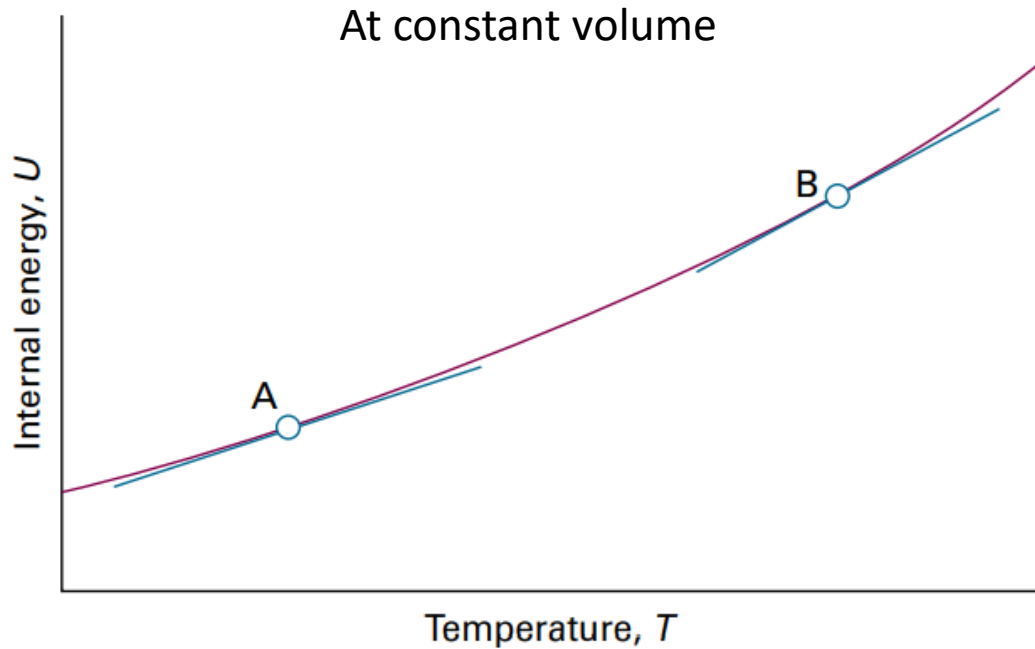
U vs T



The internal energy is only a function of temperature for perfect gases (assuming constant number of moles)

For real gases, U depends on volume

Heat capacity



The internal energy is only a function of temperature for perfect gases (assuming constant number of moles)

For real gases, U depends on volume

$$C_V = \left(\frac{\partial U}{\partial T} \right)_V$$

Molar heat capacity and specific heat capacity

$$C_V = \left(\frac{\partial U}{\partial T} \right)_V$$

extensive

Molar heat capacity and specific heat capacity

$$C_V = \left(\frac{\partial U}{\partial T} \right)_V$$

extensive

$$C_{V,m} = C_V/n$$

$$C_{V,s} = C_V/m$$

intensive

Internal energy and heat capacity

$$C_V = \left(\frac{\partial U}{\partial T} \right)_V \longrightarrow dU = C_V dT$$

Internal energy
change on heating
[constant volume]

Internal energy and heat capacity

$$C_V = \left(\frac{\partial U}{\partial T} \right)_V \longrightarrow dU = C_V dT$$

Internal energy
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$$\Delta U = \int_{T_1}^{T_2} C_V dT$$

Internal energy and heat capacity

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Internal energy
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$$\Delta U = \int_{T_1}^{T_2} C_V dT = C_V \int_{T_1}^{T_2} dT = C_V \overbrace{(T_2 - T_1)}^{\Delta T}$$

$$\Delta U = C_V \Delta T$$

Focus 2: The First Law

Internal Energy

Enthalpy

Thermochemistry

State functions

Adiabatic changes

Enthalpy

$$H = U + pV$$

Enthalpy
[definition]

Enthalpy

$$H = U + pV$$

Enthalpy
[definition]

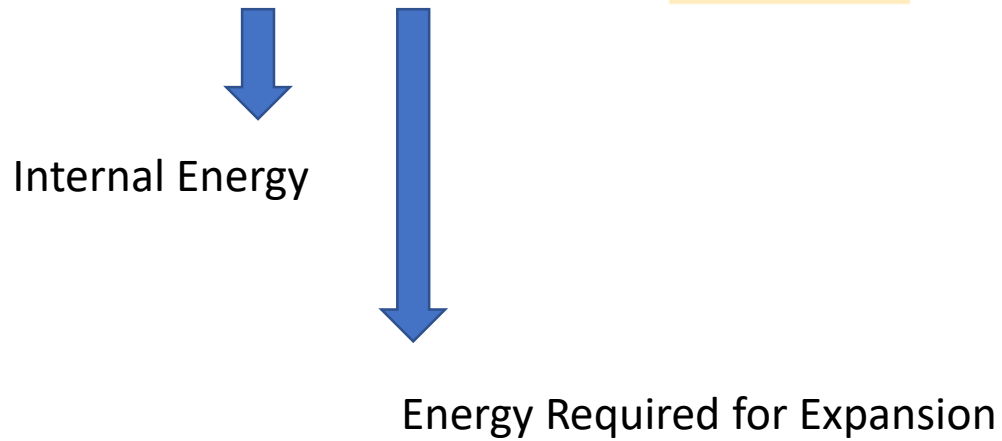


Internal Energy



Energy Required for Expansion

Enthalpy

$$H = U + pV$$


Internal Energy

Energy Required for Expansion

Enthalpy
[definition]

- In many practical situations, such as chemical reactions, phase changes, and industrial processes, systems often operate under constant pressure. When a system expands, it performs work on the surroundings, expressed as $W = p\Delta V$.
- Since a portion of the energy input is used for this expansion work, the total energy change must account for both U and pV , leading to the above relationship.

Enthalpy

$$H = U + pV$$

Enthalpy
[definition]

The change in enthalpy is equal to the energy supplied as heat at constant pressure

Enthalpy

$$H = U + pV$$

Enthalpy
[definition]

$$H + dH:$$

Enthalpy

$$H = U + pV$$

Enthalpy
[definition]

$$H + dH = (U + dU) + (p + dp)(V + dV)$$

Enthalpy

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Enthalpy
[definition]

$$H + dH = (U + dU) + (p + dp)(V + dV)$$

$$= U + dU + pV + pdV + Vdp + dpdV$$

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$$dU = dq + dw$$

Enthalpy

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Enthalpy
[definition]

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$$dU = dq + dw$$

$$dH = dq + dw + pdV + Vdp$$

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Enthalpy
[definition]

$$\begin{aligned} H + dH &= (U + dU) + (p + dp)(V + dV) \\ &= U + dU + pV + pdV + Vdp + dpdV \\ &= H + dU + pdV + Vdp \end{aligned}$$

$$dH = dU + pdV + Vdp$$



$$dU = dq + dw$$

$$dH = dq + dw + pdV + Vdp$$

If the system is in mechanical equilibrium with its surroundings at a pressure p and does only expansion work

$$dw = -pdV,$$

Enthalpy

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Enthalpy
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$$dH = dq_p$$

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If the system is in mechanical equilibrium with its surroundings at a pressure p and does only expansion work

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$$dH = dq + Vdp$$

At constant pressure, $dp = 0$,

$$dH = dq_p$$

If no additional work done, the change in enthalpy is equal to the energy supplied as heat at constant pressure

Measurable enthalpy change

$$dH = dq_p$$

Measurable enthalpy change

$$dH = dq_p$$

$$\overbrace{\int_i^f dH}^{H_f - H_i} = \overbrace{\int_i^f dq}^{q_p}$$

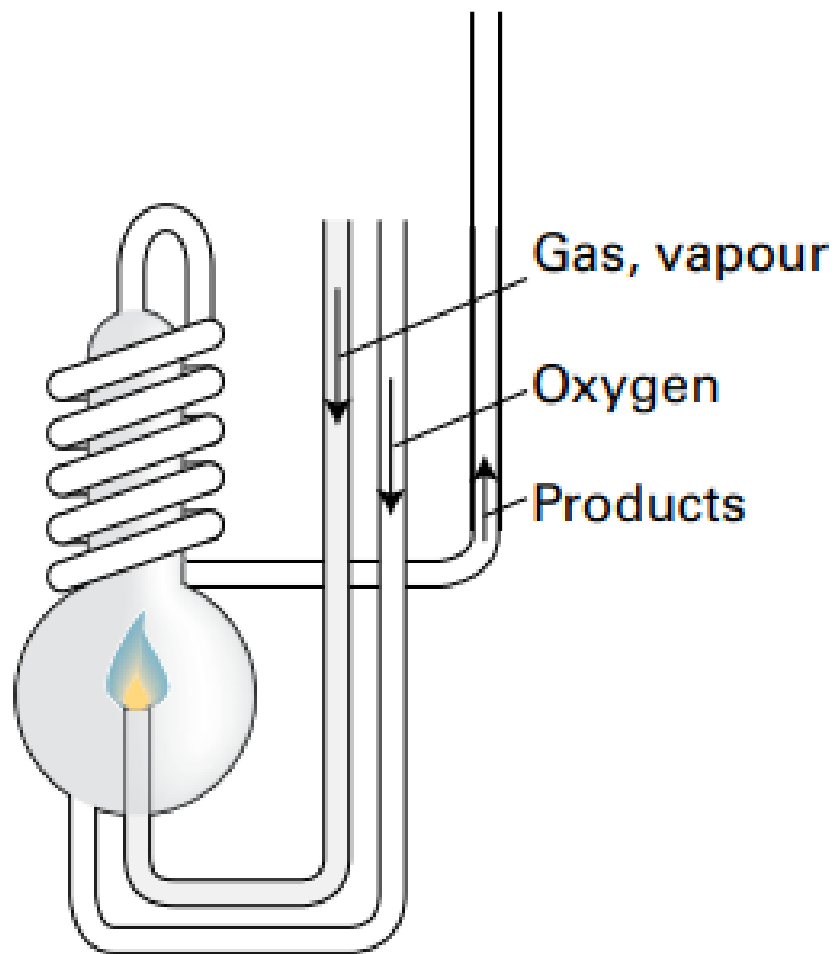
Measurable enthalpy change

$$dH = dq_p$$

$$\overbrace{\int_i^f dH}^{H_f - H_i} = \overbrace{\int_i^f dq}^{q_p} \quad \longrightarrow \quad \Delta H = q_p$$

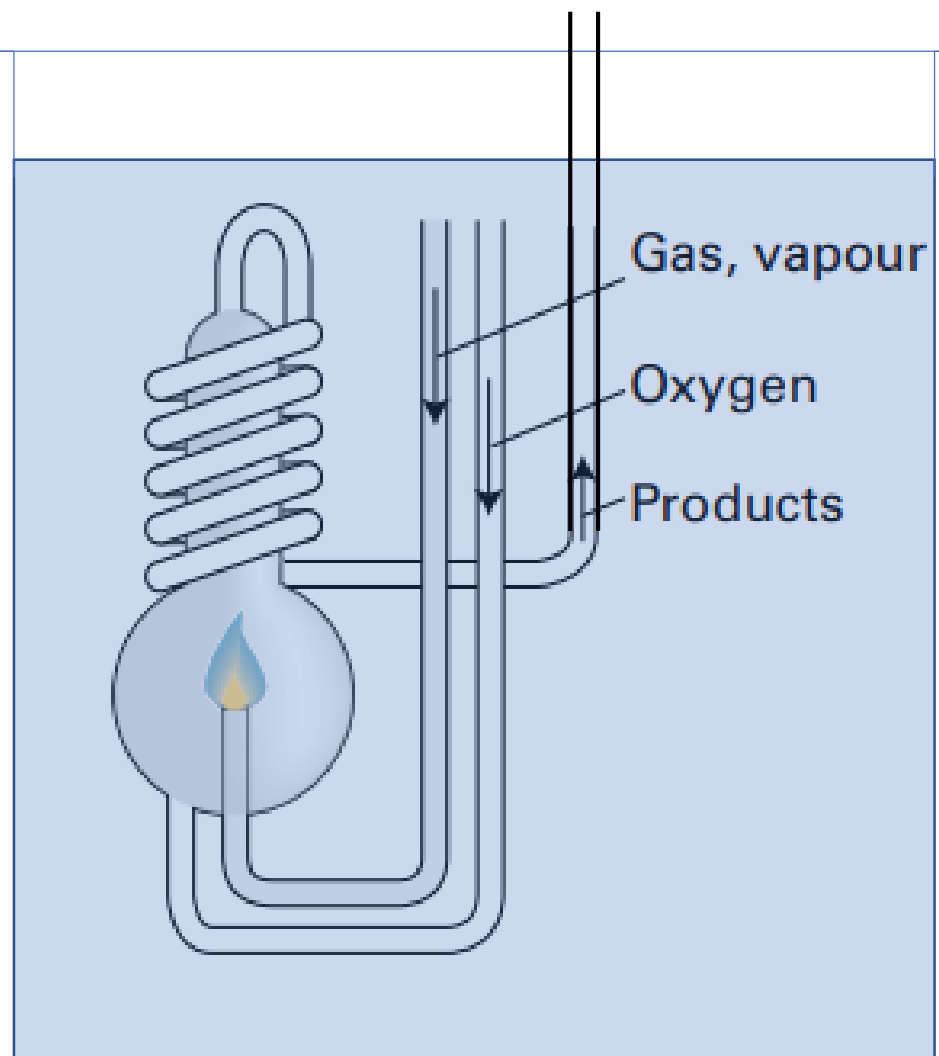
Heat transferred at
constant pressure
[measurable change]

Isobaric Calorimetry



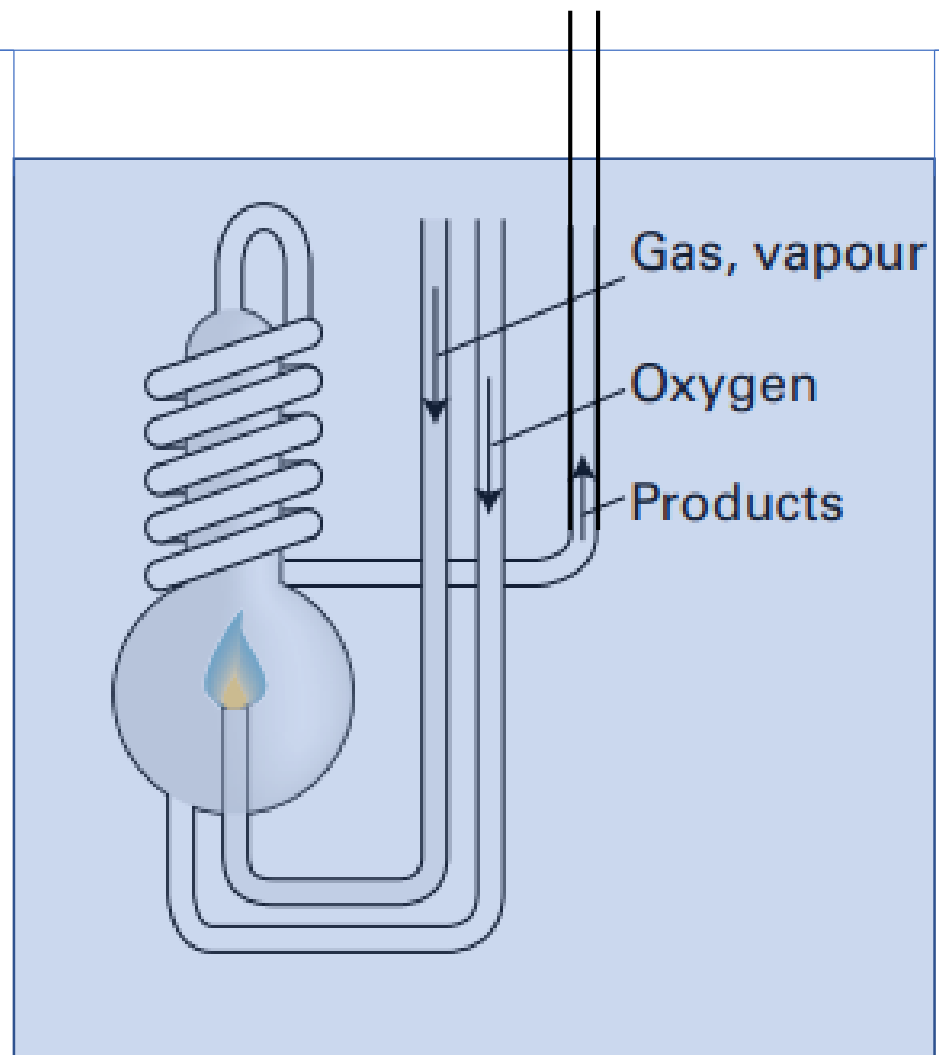
A constant pressure flame calorimeter

Isobaric Calorimetry



A constant pressure flame calorimeter

Isobaric Calorimetry



A constant pressure flame calorimeter



Enthalpy of a perfect gas

Enthalpy
[definition]

$$H = U + pV$$

Enthalpy of a perfect gas

Enthalpy
[definition]

$$H = U + pV$$

For
perfect
gases



$$H = U + pV = U + nRT$$

Enthalpy

Enthalpy
[definition]

$$H = U + pV$$

For
perfect
gases



$$H = U + pV = U + nRT$$

The change of enthalpy in a reaction that produces or consumes gas under isothermal conditions

$$\Delta H = \Delta U + \Delta n_{\text{g}} RT$$

Enthalpy

Enthalpy
[definition]

$$H = U + pV$$

For
perfect
gases



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change in the number of moles of
gas molecules in the reaction

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change in the number of moles of
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$$\Delta n_g = -3$$

Enthalpy

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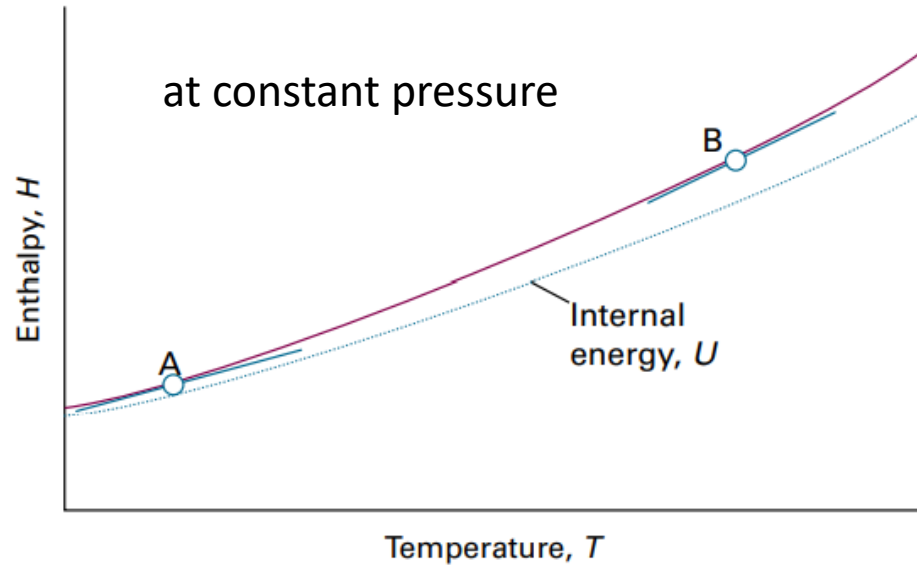


$$\Delta n_g = -3$$

$$\Delta H - \Delta U = (-3) \times RT \approx -7.5 \text{ kJ mol}^{-1}$$

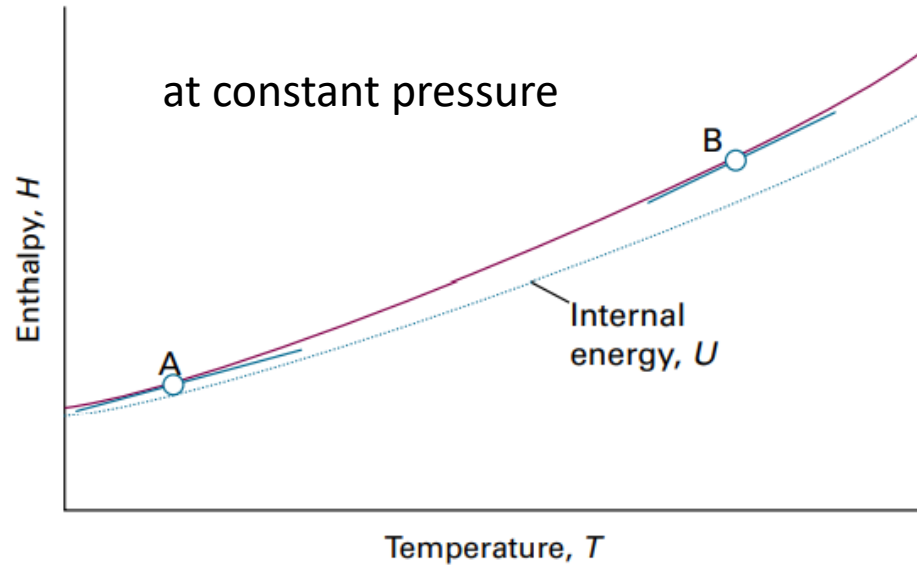
Enthalpy as a function of temperature

The enthalpy of a substance increases as its temperature is raised



Enthalpy as a function of temperature

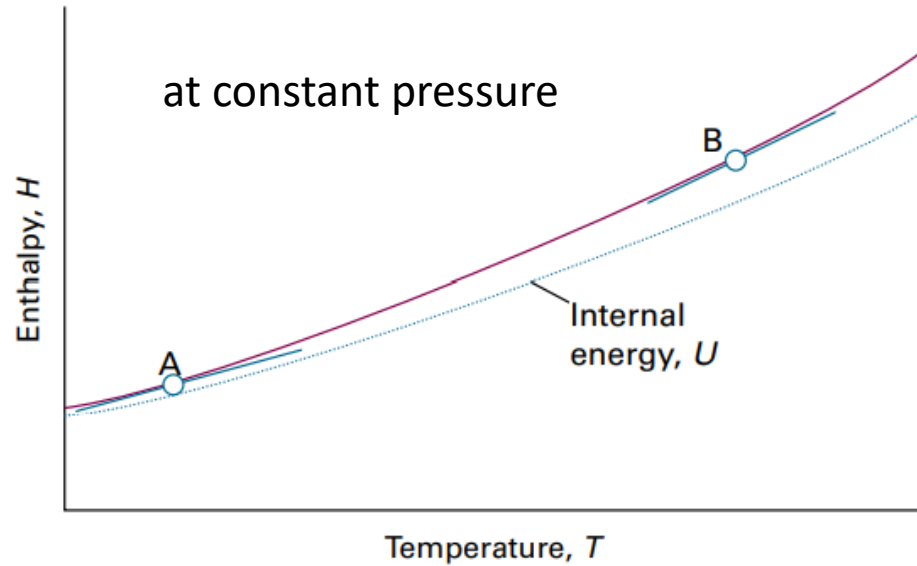
The enthalpy of a substance increases as its temperature is raised



$$C_p = \left(\frac{\partial H}{\partial T} \right)_p$$

Enthalpy as a function of temperature

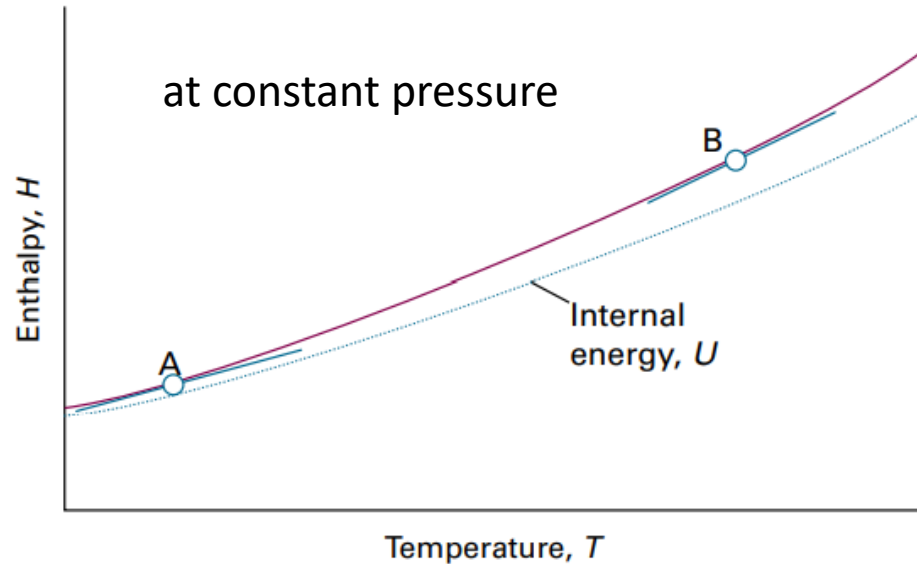
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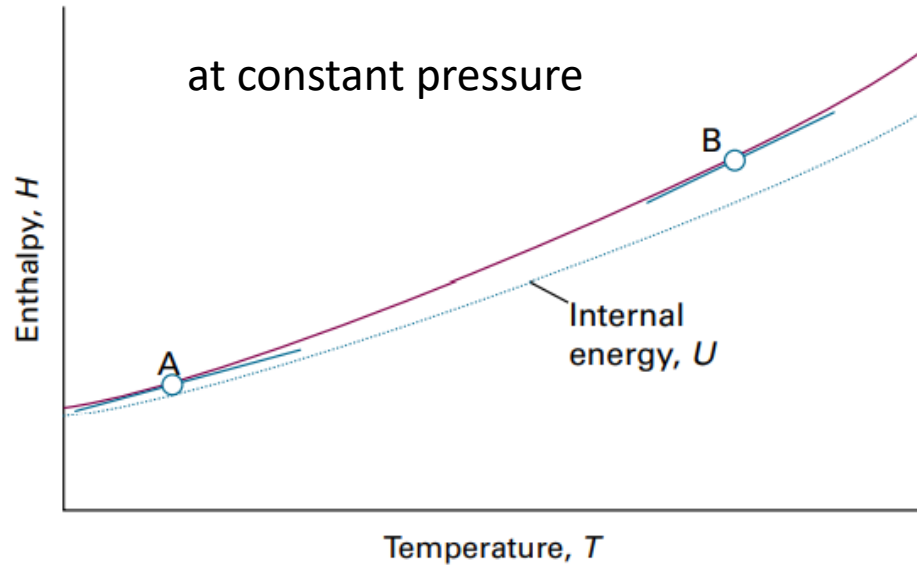


$$C_p = \left(\frac{\partial H}{\partial T} \right)_p \longrightarrow dH = C_p dT$$

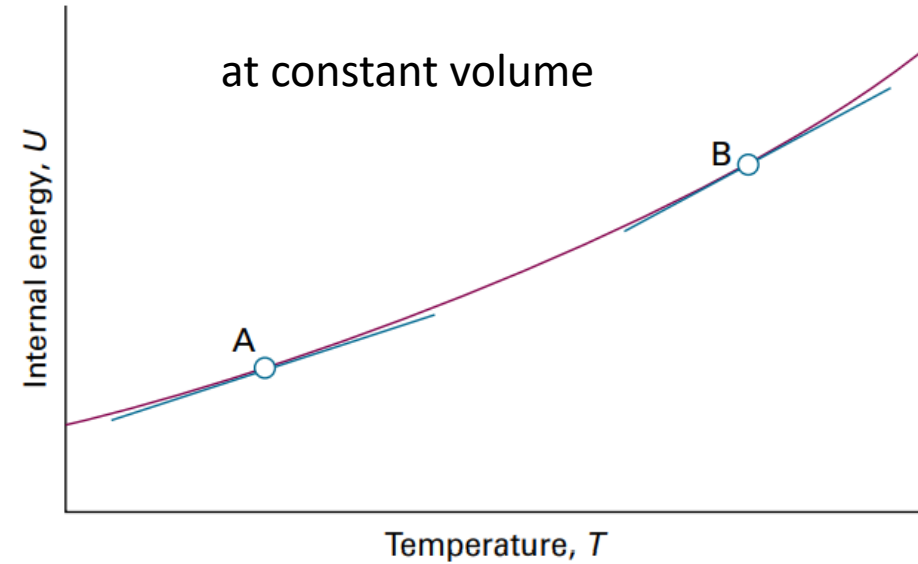
If the heat capacity is constant,

$$\begin{aligned} \Delta H &= \int_{T_1}^{T_2} C_p dT = C_p \int_{T_1}^{T_2} dT = C_p \overbrace{(T_2 - T_1)}^{\Delta T} \\ &= C_p \Delta T \end{aligned}$$

C_p and C_v



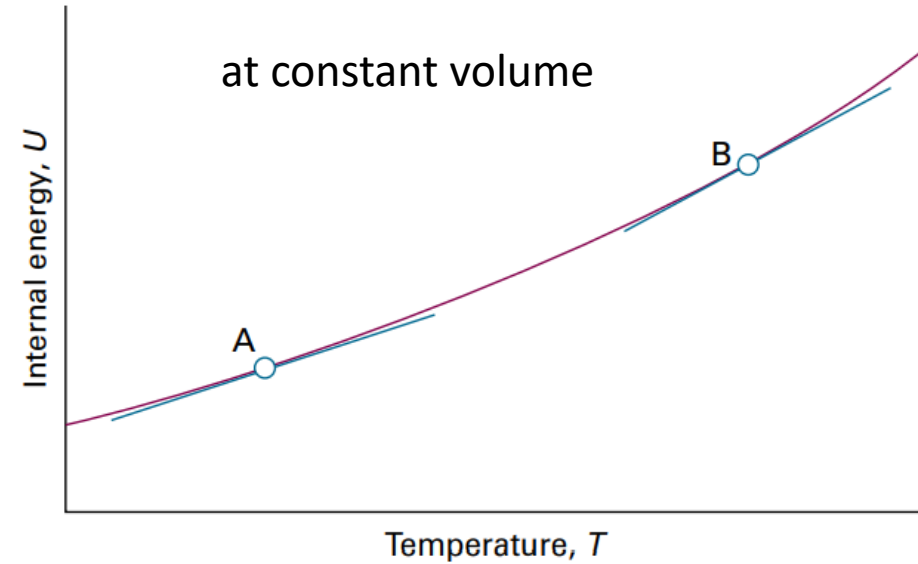
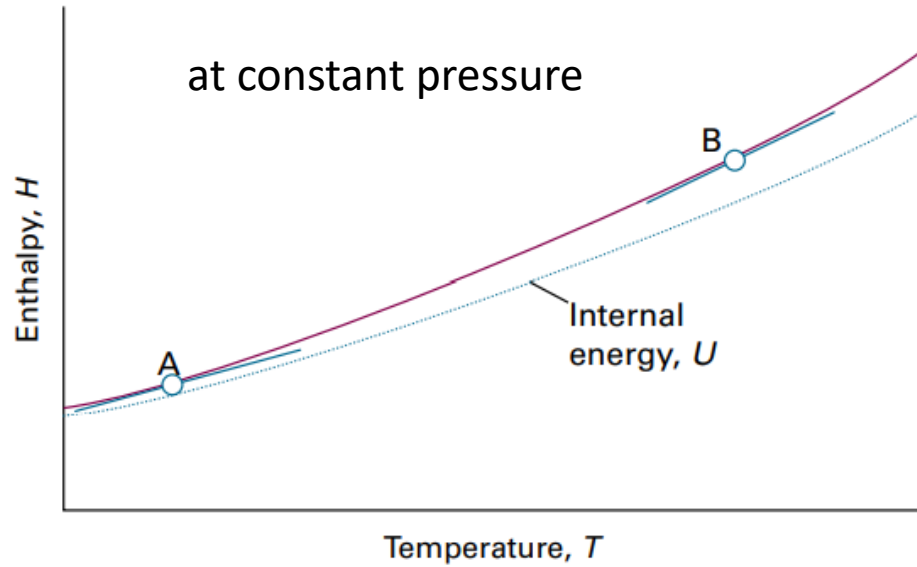
$$C_p = \left(\frac{\partial H}{\partial T} \right)_p$$



$$C_v = \left(\frac{\partial U}{\partial T} \right)_v$$

At constant pressure, the system expands and does work on the surroundings, requiring more heat to achieve the same temperature change compared to constant volume conditions.

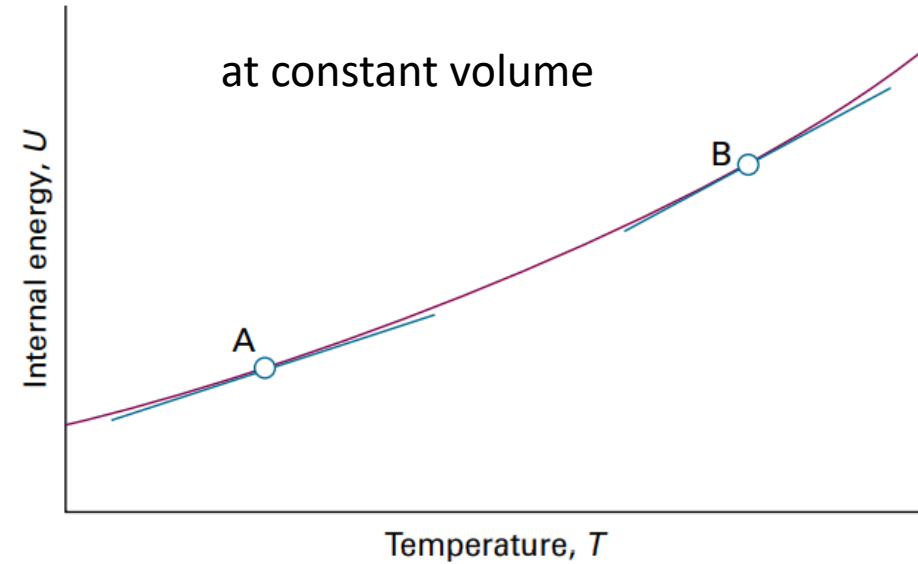
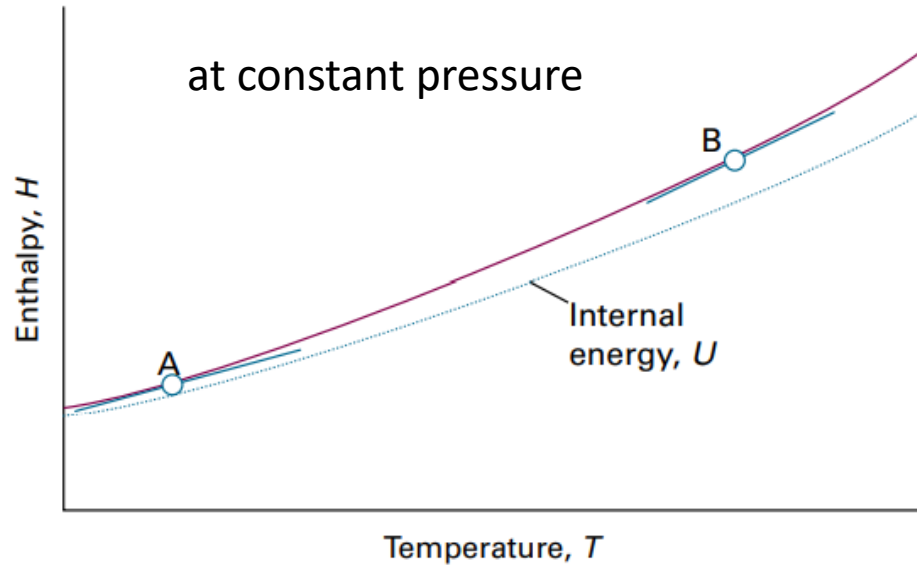
C_p and C_v



$$C_p = \left(\frac{\partial H}{\partial T} \right)_p > C_v = \left(\frac{\partial U}{\partial T} \right)_v$$

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C_p and C_v



$$C_p = \left(\frac{\partial H}{\partial T} \right)_p > C_v = \left(\frac{\partial U}{\partial T} \right)_v$$

perfect gas: $C_p - C_v = nR$

$$R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$$
$$= 0.08205 \text{ L atm mol}^{-1} \text{ K}^{-1}$$