



2016 Kinematics Summer School

Static Balancing of Compliant Mechanisms (SBCM)

Just Herder



Quale é stato il principio fondamentale di tutte le mie realizzazioni?

Si spiega con una sola parola:

-Semplicità- portata all'estremo possibile.

What is the fundamental principle of all my creations?

That comes down to a single motto:

-Simplicity- pushed to the farthest extremes.

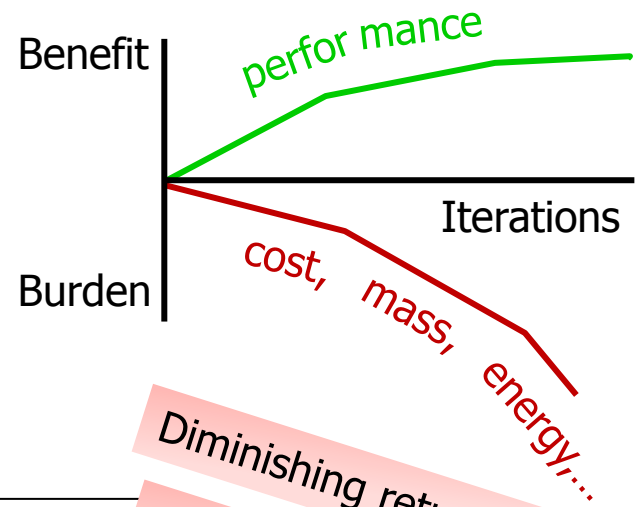


Fundamental design

System performs less than sum of parts



Analysis tools well developed, synthesis still in infancy



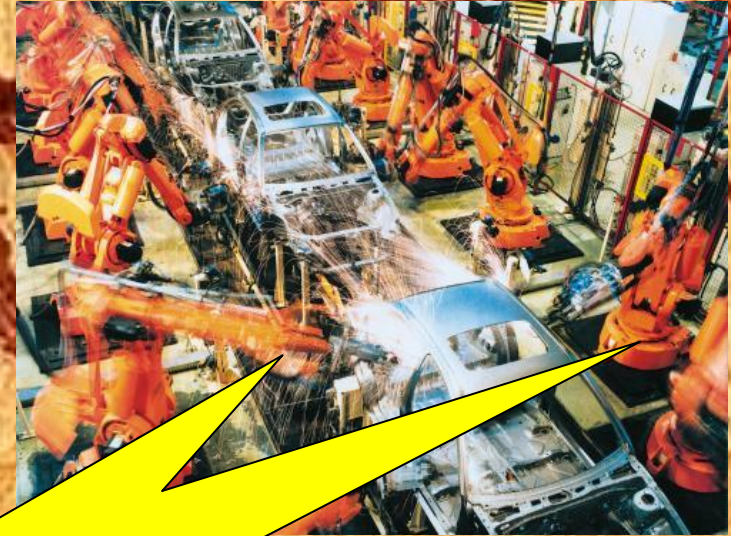
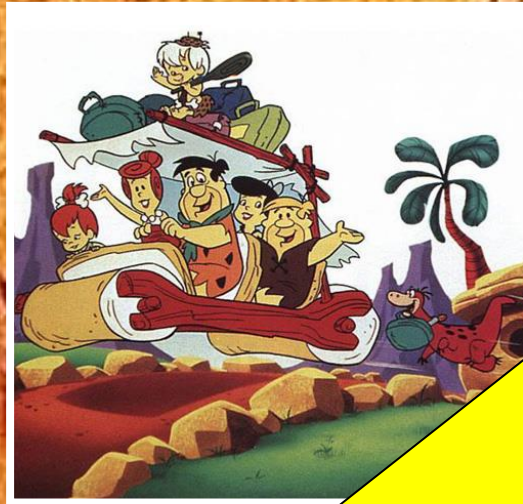
Diminishing return

Side-effects grow faster

Concept \longleftrightarrow Behavior \longrightarrow Performance

Minimal \longleftarrow Essence

Earliest mechanisms

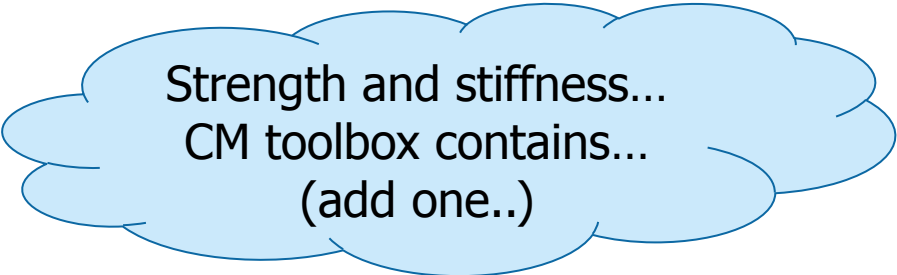


Doing the wrong thing
better and better...



Cave paintings in Valltorta Gorge, Spain, 20,000 BC
Kuka Robotics, TAG Heuer

Quiz



Strength and stiffness...
CM toolbox contains...
(add one..)

Ever designed a linkage mechanism?

Ever designed a compliant mechanism?

Advantages compliant mechanisms?

Disadvantages compliant mechanisms?

Compliant mechanisms

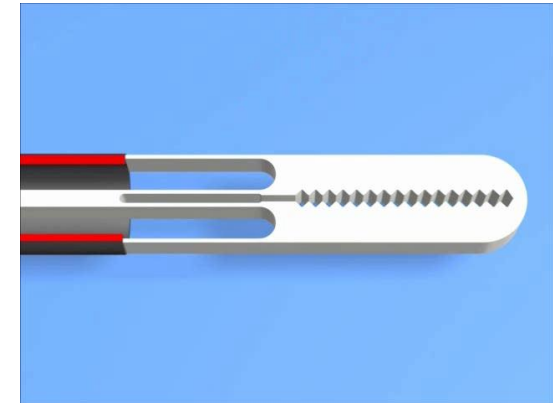
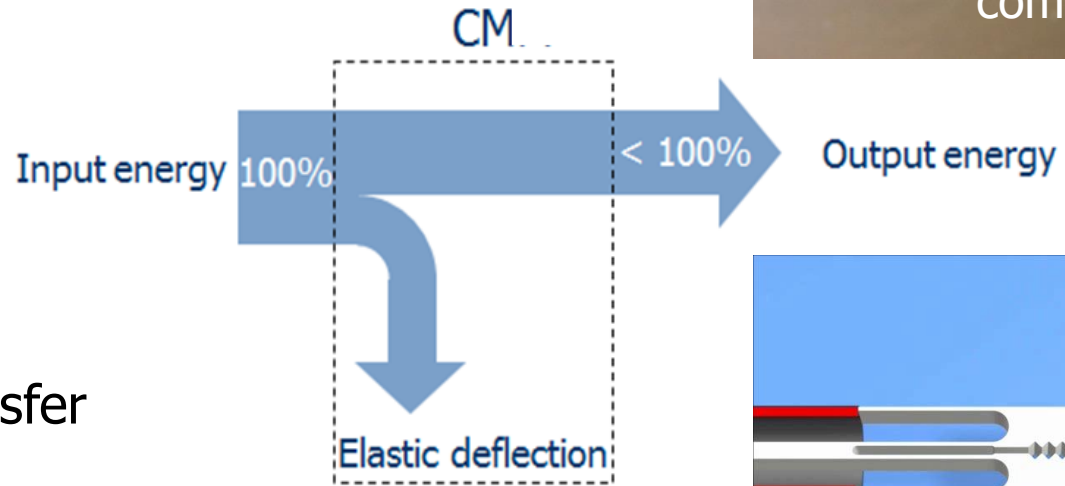
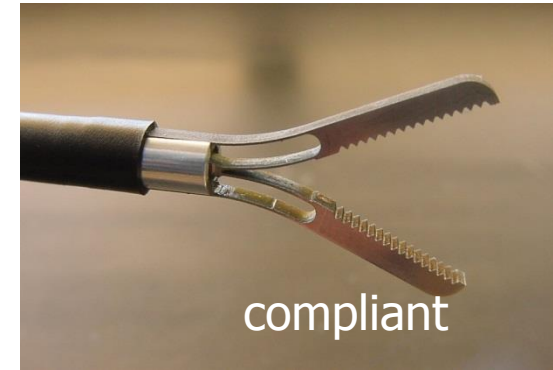
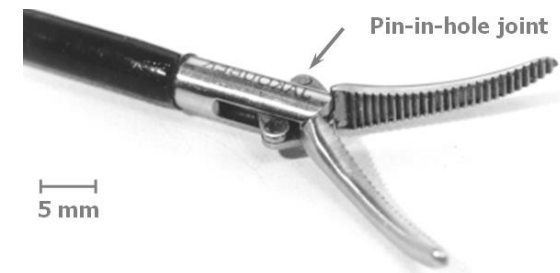
- Inherently soft and slender
- Low mass
- No assembly
- No friction or backlash
- No lubrication (clean, vacuum)
- Down-scalable
- ...

But

- Poor efficiency
- Poor force transfer

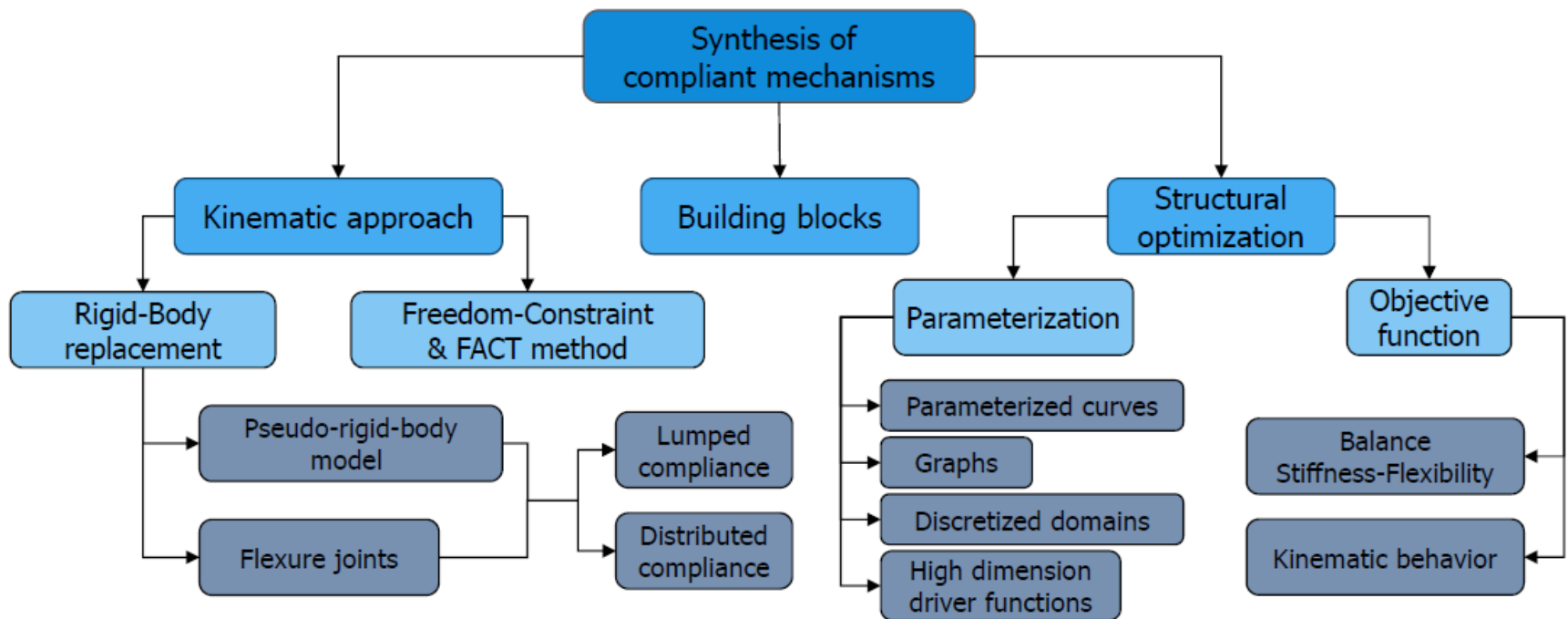
Hooke's law: $\sigma = E\varepsilon$

Stiffness: $F = kx$



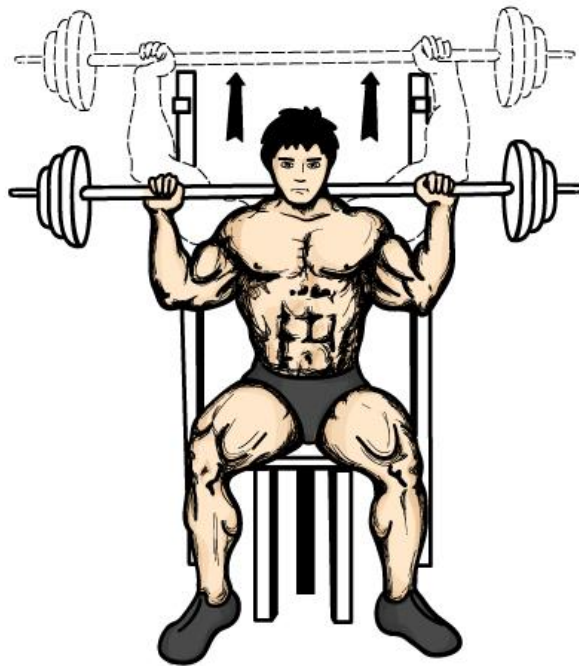
Today

- ▶ Static balancing
- ▶ Static balancing of compliant mechanisms
- ▶ Mainly rigid body replacement



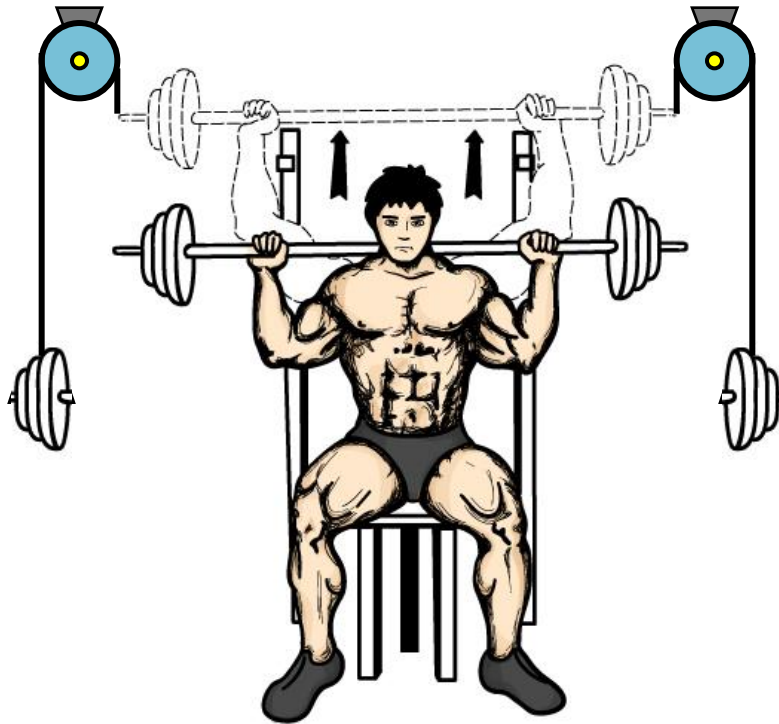
Weight lifting

- Requires doing work...



Weight lifting

- Requires doing work... or does it not?



Draw bridge

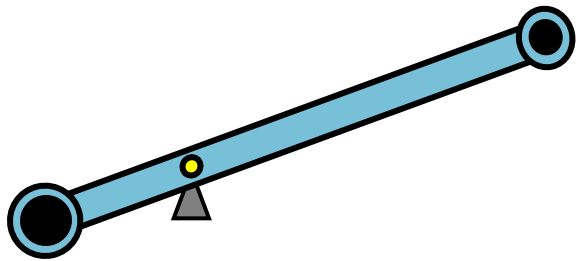


Draw bridge

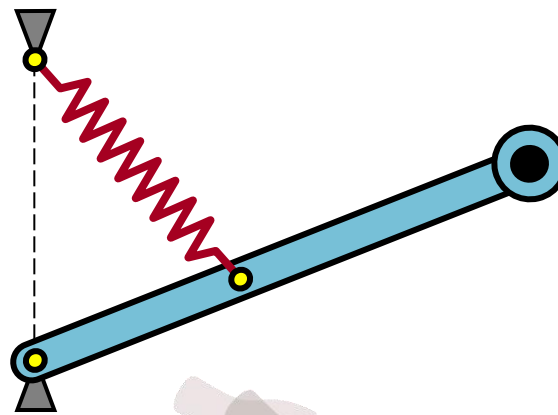


Static Balancing

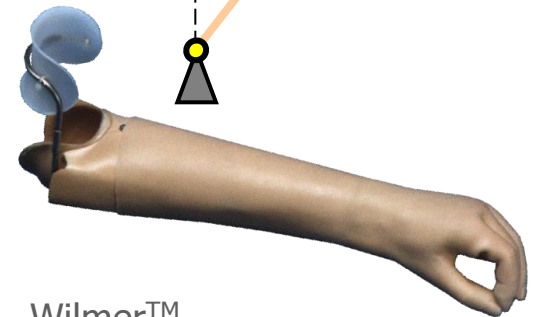
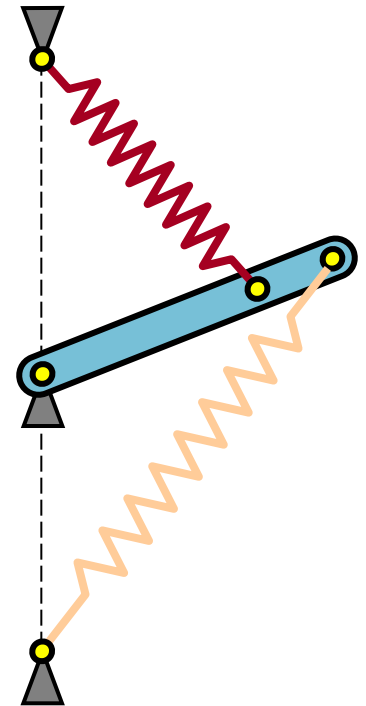
All conservative forces can be cancelled out!



Meager Bridge (Amsterdam)



Anglepoise™

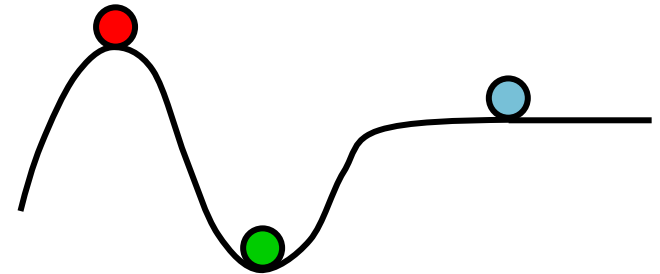


Wilmer™

Static Balancing

All conservative forces can be cancelled out!

- Continuous equilibrium
- Constant potential energy
- Neutral stability



Meager Bridge (Amsterdam)

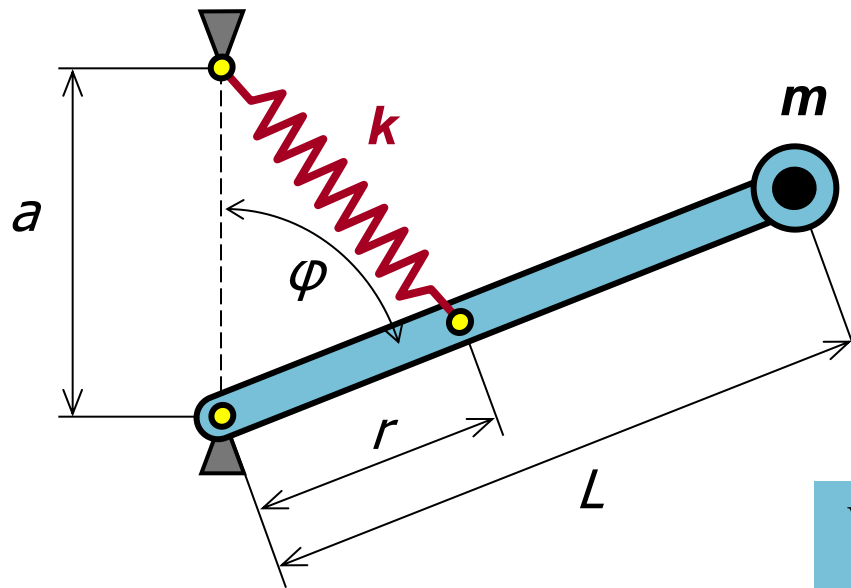


Anglepoise™



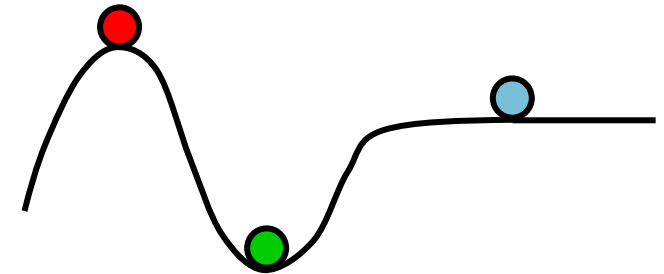
Wilmer™

Constant potential energy



Assuming zero-free-length (ZFL) springs:

$$\bar{F} = k\bar{\ell}$$



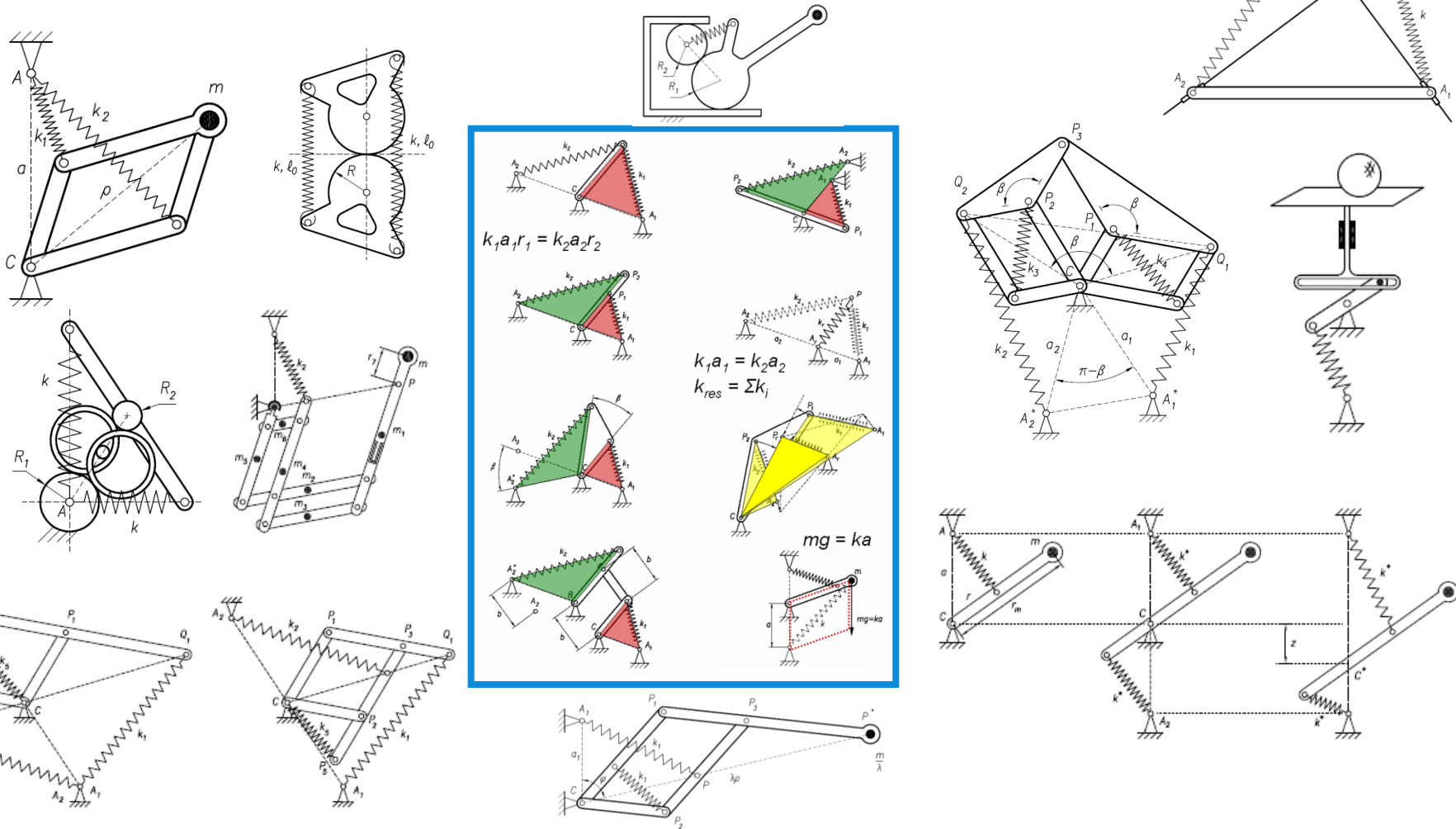
$$V_m = mgL \cos \varphi$$

$$V_s = \frac{1}{2} k \ell^2 = \frac{1}{2} k (a^2 + r^2) - kar \cos \varphi$$

$$V_{tot} = cnst + (mgL - kar) \cos \varphi$$

Condition : $mgL = kar$

Conceptual design, framework





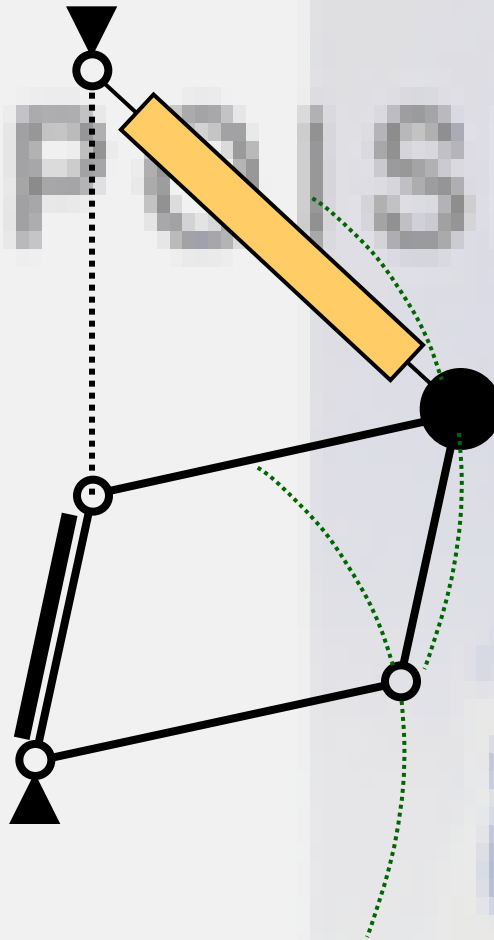
Terry's
ANGLEPOISE
LAMP

*Light at any Angle
at a
Finger Touch*



PATENTED AT HOME AND ABROAD

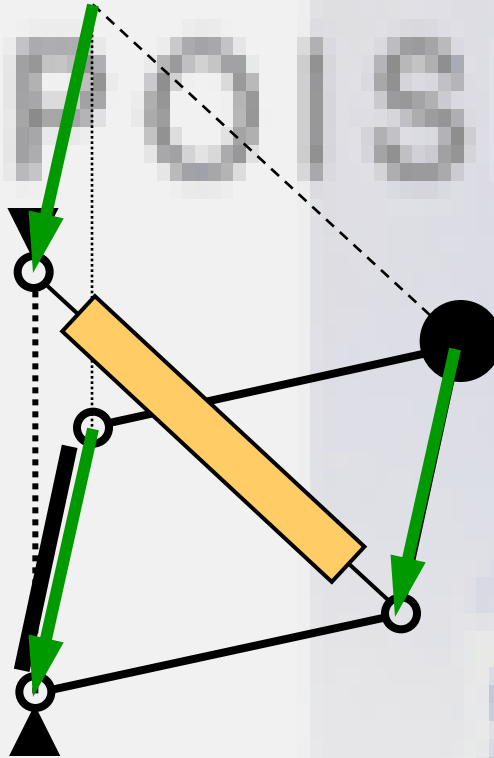
ANGLE POSITION



$$mgL_1 = r_1 k_1 a_1$$

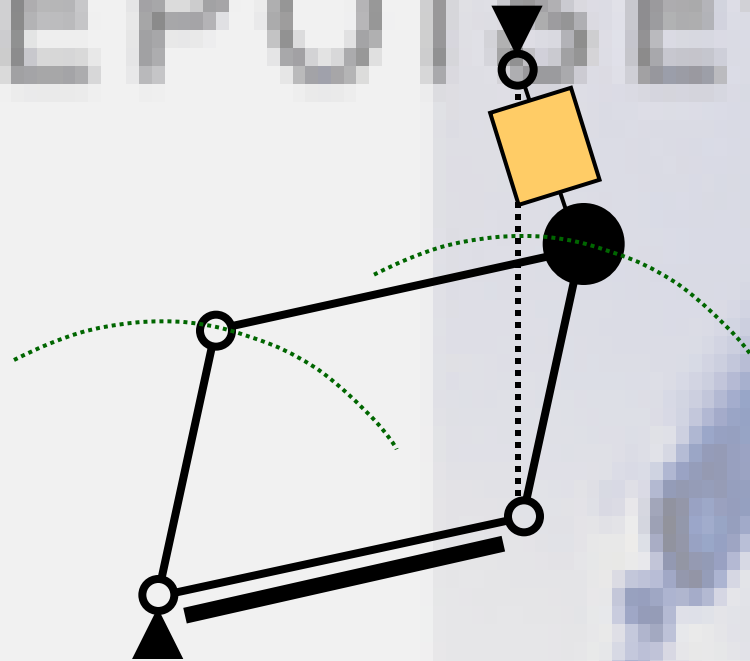
Superposition:
first degree of freedom

ANGLE POISE



Modification:
shift of spring element

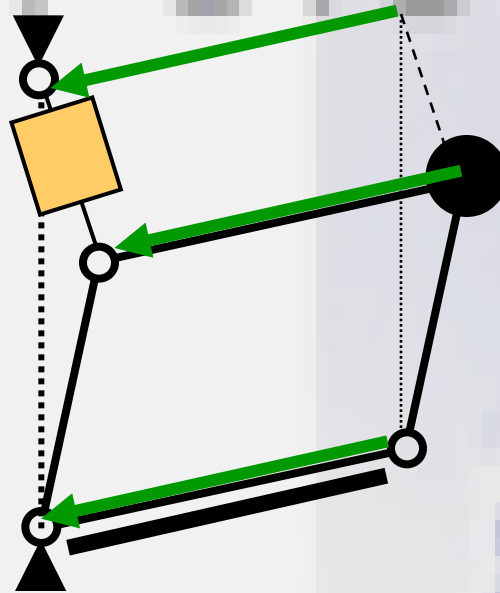
ANGLE POISED



$$mgL_2 = r_2 k_2 a_2$$

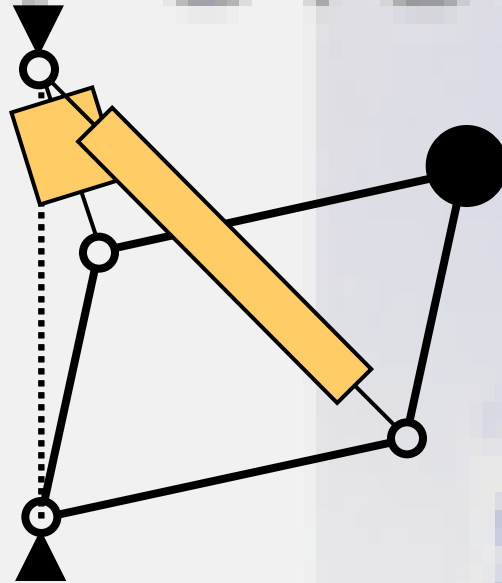
Superposition:
second degree of
freedom

ANGLE POISE



Modification:
shift of spring element

ANGLE POISE



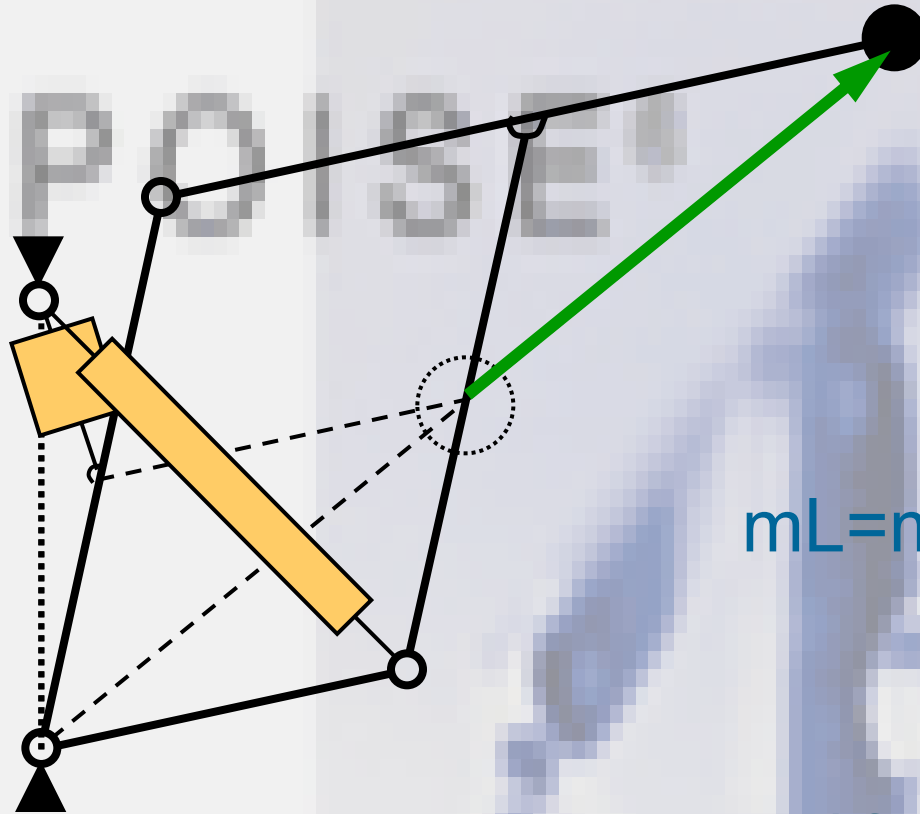
$$mgL_1 = r_1 k_1 a_1$$

$$mgL_2 = r_2 k_2 a_2$$

Superposition:

combination of the
two degrees of
freedom

ANGLE POISED

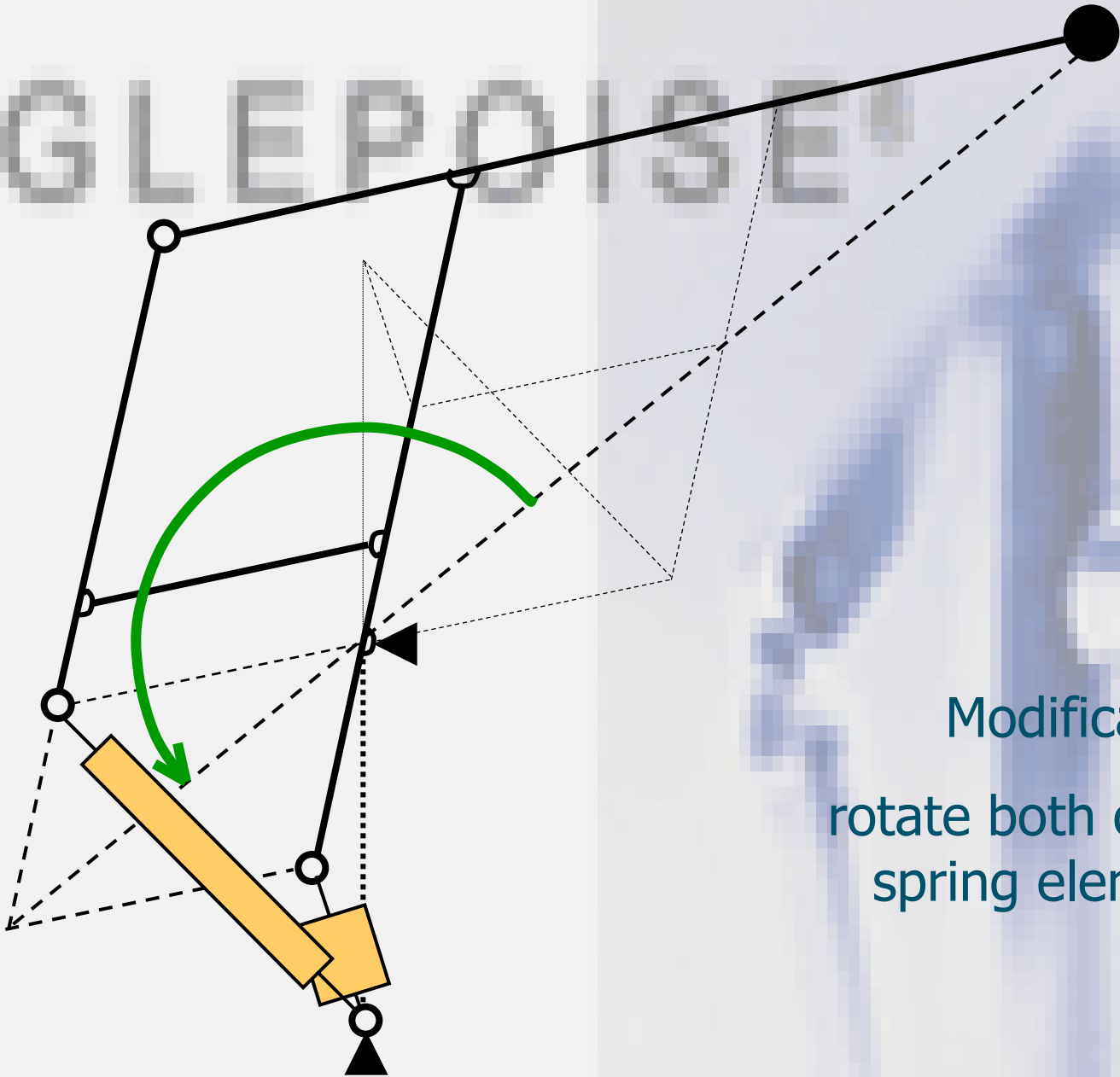


$$mL = m'L'$$

Modification:

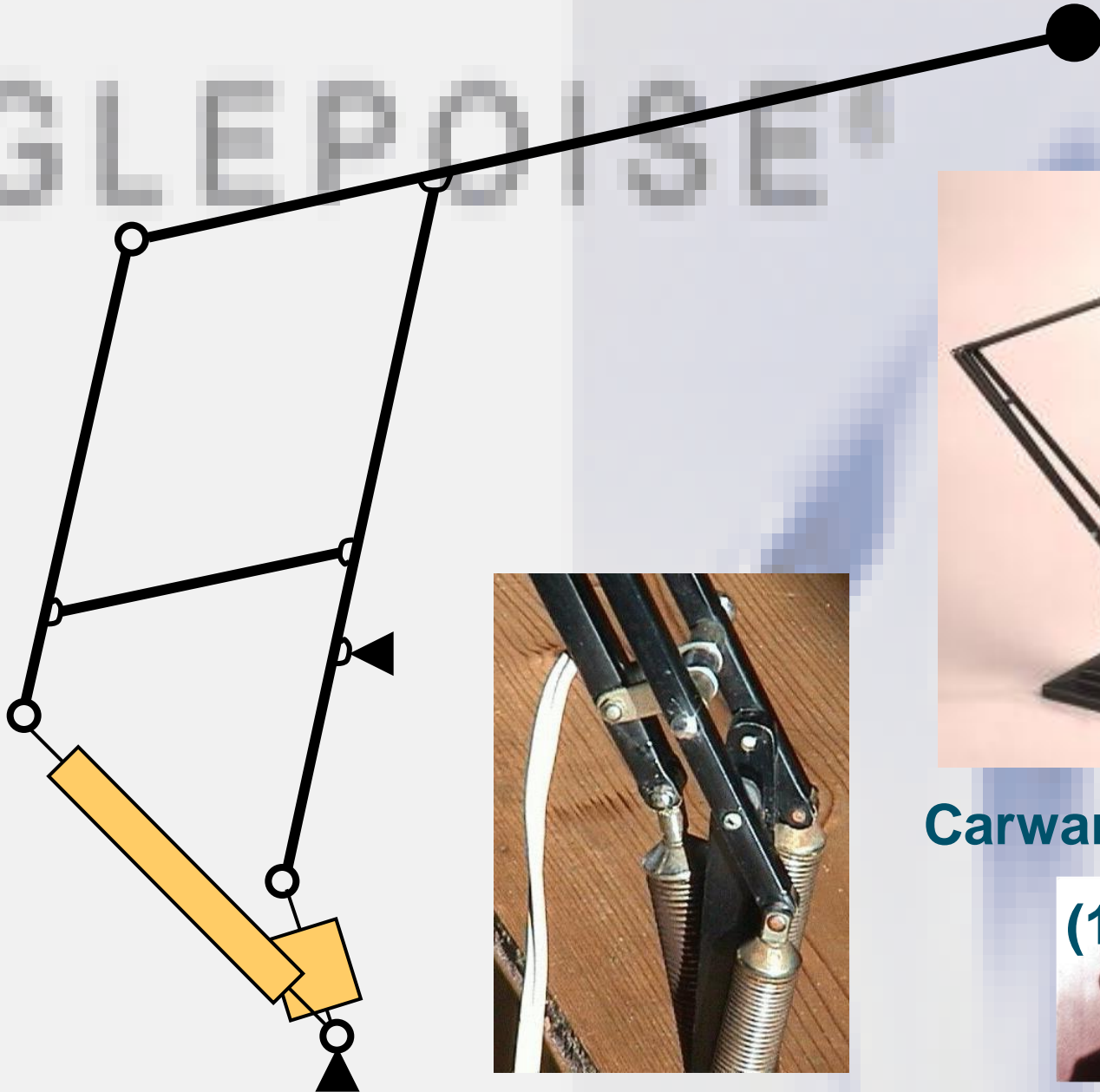
elongate lever while
reducing mass

ANGLEPOISED



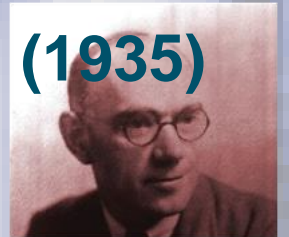
Modification:
rotate both of the
spring elements

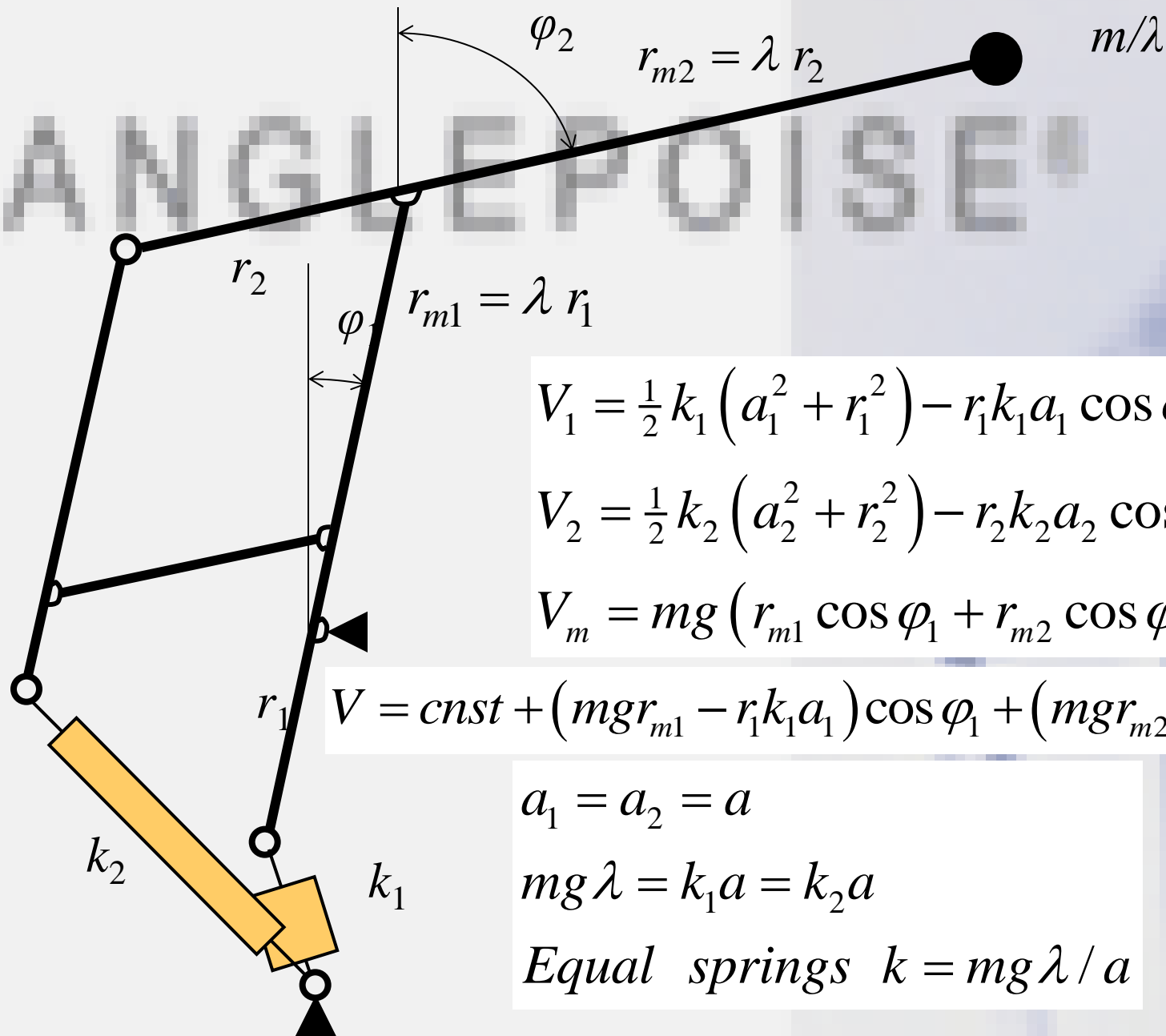
ANGLEPOISE



Carwardine

(1935)





ANGLEPOISE!

$$V_1 = \frac{1}{2} k_1 (a_1^2 + r_1^2) - r_1 k_1 a_1 \cos \varphi_1$$

$$V_2 = \frac{1}{2} k_2 (a_2^2 + r_2^2) - r_2 k_2 a_2 \cos \varphi_2$$

$$V_m = mg (r_{m1} \cos \varphi_1 + r_{m2} \cos \varphi_2)$$

$$V = \text{const} + (mgr_{m1} - r_1 k_1 a_1) \cos \varphi_1 + (mgr_{m2} - r_2 k_2 a_2) \cos \varphi_2$$

$$a_1 = a_2 = a$$

$$mg \lambda = k_1 a = k_2 a$$

$$\text{Equal springs } k = mg \lambda / a$$

John Terry and several lamp generations

ANGLEPOISE®



ANGLEPOISE®

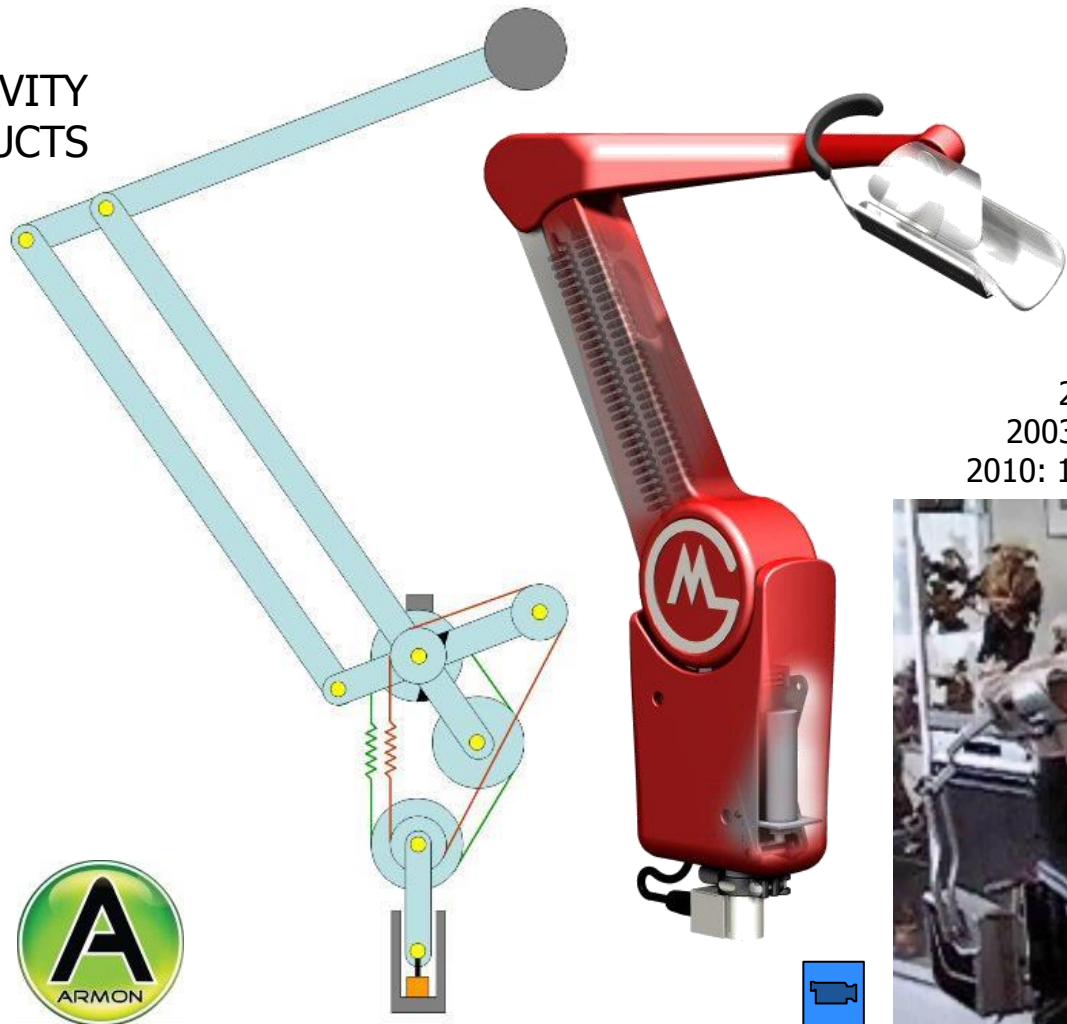


Type 3

www.anglepoise.com

Past work: Armon mobile arm support

MICROGRAVITY
PRODUCTS



2001: MSc projects
2003: MGP established
2010: 150 units produced

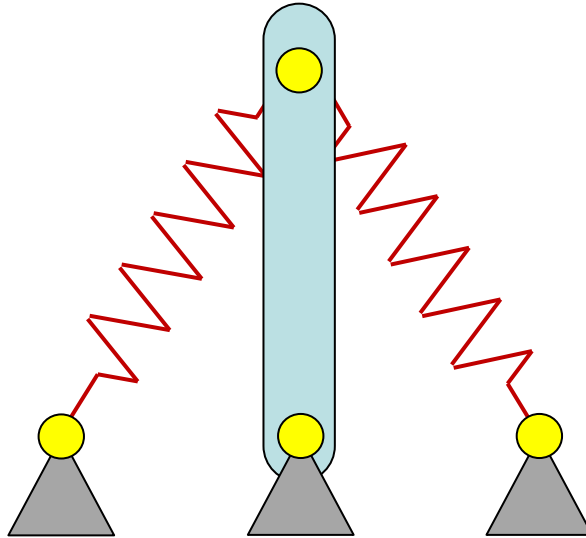


Zero-gravity force environment

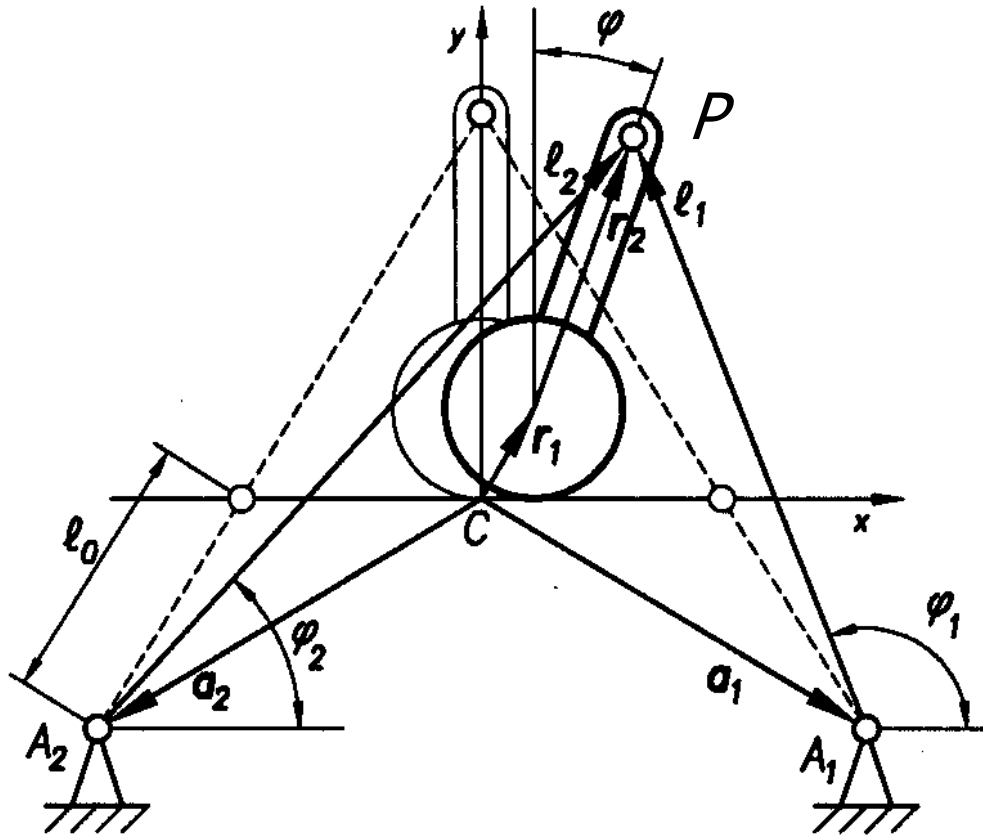


Extended vector loop closure

1. Start with ZFL solution



Extended vector loop closure



In this case two loops, one for each spring

1. Start with ZFL solution
2. Replace ZFL by normal springs (l_0)
3. Apply rolling contact joint (optional)
4. Extend vector loop with energy eq.:

$$a_1 + l_1 = r_1 + r_3$$

$$a_2 + l_2 = r_1 + r_3$$

$$V_1 + V_2 = K$$

Extended vector loop closure

$$0 = A_x + R\varphi_i + r_2 \sin \varphi_i + \ell_{1,i} \cos \varphi_{1,i}$$

$$0 = A_y + R + r_2 \cos \varphi_i - \ell_{1,i} \sin \varphi_{1,i}$$

$$0 = -A_x - R\varphi_i - r_2 \sin \varphi_i + \ell_{2,i} \cos \varphi_{2,i}$$

$$0 = A_y + R + r_2 \cos \varphi_i - \ell_{2,i} \sin \varphi_{2,i}$$

$$0 = \frac{1}{2}k(\ell_{1,i} - \ell_{01})^2 + \frac{1}{2}k(\ell_{2,i} - \ell_{02})^2 - K$$

$$a_1 + \ell_1 = r_1 + r_3$$

$$a_2 + \ell_2 = r_1 + r_3$$

$$V_1 + V_2 = K$$

Extended vector loop closure

$$0 = A_x + R\varphi_i + r_2 \sin \varphi_i + \ell_{1,i} \cos \varphi_{1,i}$$

$$0 = A_y + R + r_2 \cos \varphi_i - \ell_{1,i} \sin \varphi_{1,i}$$

$$0 = -A_x - R\varphi_i - r_2 \sin \varphi_i + \ell_{2,i} \cos \varphi_{2,i}$$

$$0 = A_y + R + r_2 \cos \varphi_i - \ell_{2,i} \sin \varphi_{2,i}$$

$$0 = \frac{1}{2}k(\ell_{1,i} - \ell_{01})^2 + \frac{1}{2}k(\ell_{2,i} - \ell_{02})^2 - K$$

1. Assume springs are preselected, then k , ℓ_{01} and ℓ_{02} are known.
2. Also preselect energy level K
3. Then **5n** equations and **10** (r_{1x} r_{2x} r_{k1x} r_{k2x} φ_{01x} φ_{02x} A_{1x} A_{1y} A_{2x} A_{2y}) + **4n** (ℓ_{1x} ℓ_{2x} ψ_{1x} ψ_{2x}) unknowns.
4. From $5n=10+4n$ we find at most 10 precision points

Extended vector loop closure

Nr of pos. (n)	Nr of scal. eqs. (5n)	Number of scalar unknowns (plus symbols) (10+4n)	Number of free choices (plus suggested symbols) (10-n)
1	5	14 $(\ell_{1,1}, \ell_{2,1}, \psi_{1,1}, \psi_{2,1}, r_1, r_2, r_{k1}, r_{k2}, \varphi_{01}, \varphi_{02}, A_{1x}, A_{1y}, A_{2x}, A_{2y})$	9 $(r_1, r_{k1}, r_{k2}, \varphi_{01}, \varphi_{02}, A_{1x}, A_{1y}, A_{2x}, A_{2y})$
2	10	18 $(above + \ell_{1,2}, \ell_{2,2}, \psi_{1,2}, \psi_{2,2})$	8 $(r_{k1}, r_{k2}, \varphi_{01}, \varphi_{02}, A_{1x}, A_{1y}, A_{2x}, A_{2y})$
3	15	22 $(above + \ell_{1,3}, \ell_{2,3}, \psi_{1,3}, \psi_{2,3})$	7 $(r_{k2}, \varphi_{01}, \varphi_{02}, A_{1x}, A_{1y}, A_{2x}, A_{2y})$
4	20	26 $(above + \ell_{1,4}, \ell_{2,4}, \psi_{1,4}, \psi_{2,4})$	6 $(\varphi_{01}, \varphi_{02}, A_{1x}, A_{1y}, A_{2x}, A_{2y})$
5	25	30 $(above + \ell_{1,5}, \ell_{2,5}, \psi_{1,5}, \psi_{2,5})$	5 $(\varphi_{02}, A_{1x}, A_{1y}, A_{2x}, A_{2y})$
6	30	34 $(above + \ell_{1,6}, \ell_{2,6}, \psi_{1,6}, \psi_{2,6})$	4 $(A_{1x}, A_{1y}, A_{2x}, A_{2y})$
7	35	38 $(above + \ell_{1,7}, \ell_{2,7}, \psi_{1,7}, \psi_{2,7})$	3 (A_{1y}, A_{2x}, A_{2y})
8	40	42 $(above + \ell_{1,8}, \ell_{2,8}, \psi_{1,8}, \psi_{2,8})$	2 (A_{2x}, A_{2y})
9	45	46 $(above + \ell_{1,9}, \ell_{2,9}, \psi_{1,9}, \psi_{2,9})$	1 (A_{2y})
10	50	50 $(above + \ell_{1,10}, \ell_{2,10}, \psi_{1,10}, \psi_{2,10})$	0

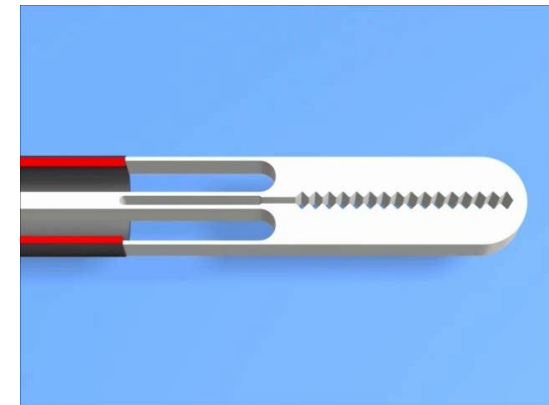
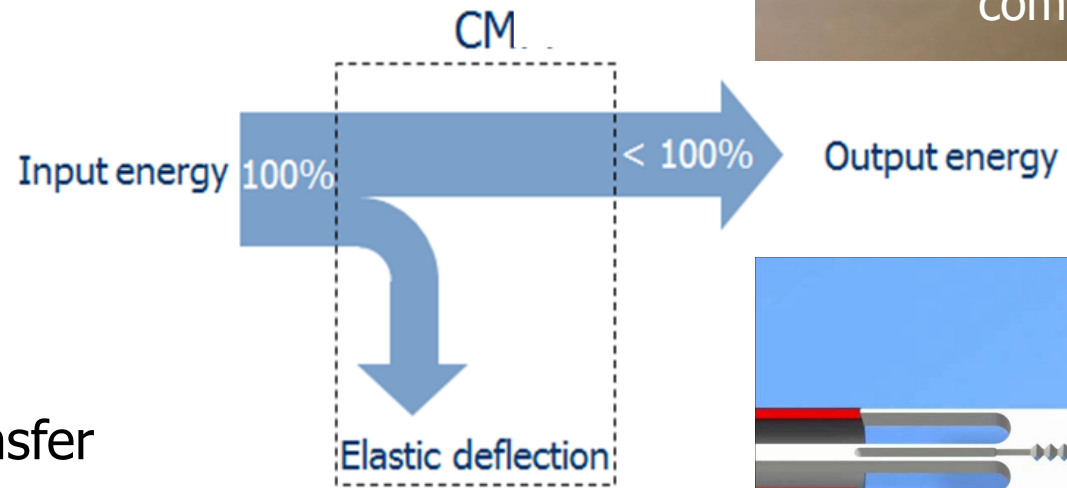
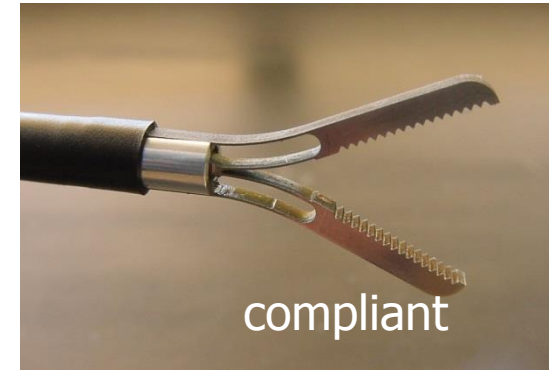
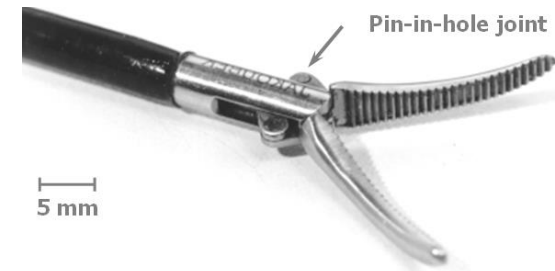
Compliant mechanisms

Monolithic

- No friction or backlash
- No lubrication
- No assembly

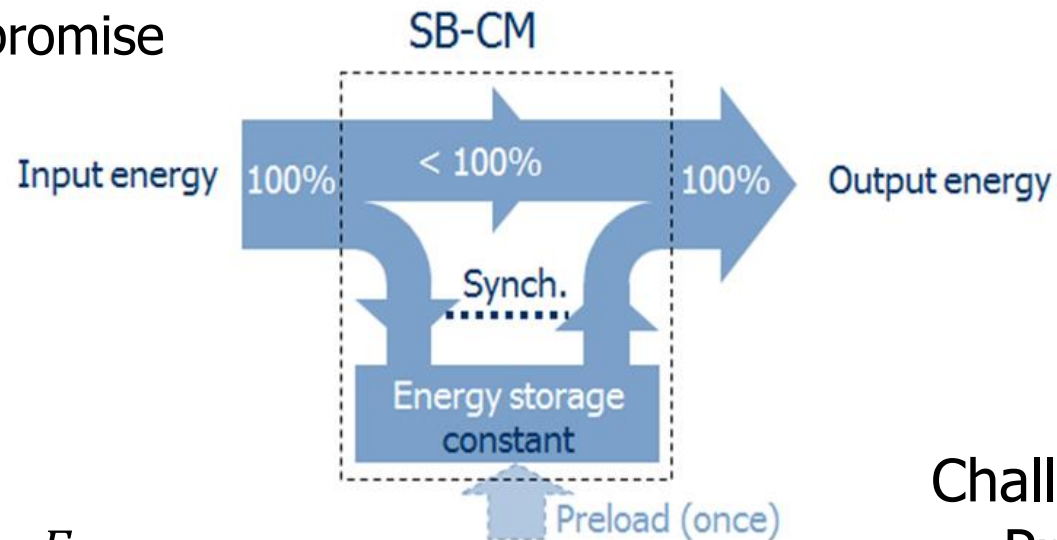
But

- Poor efficiency
- Poor force transfer



Static Balancing of Compliant Mech.

- Energy not dissipated > Balancing
- Best of both worlds!
- No longer compromise



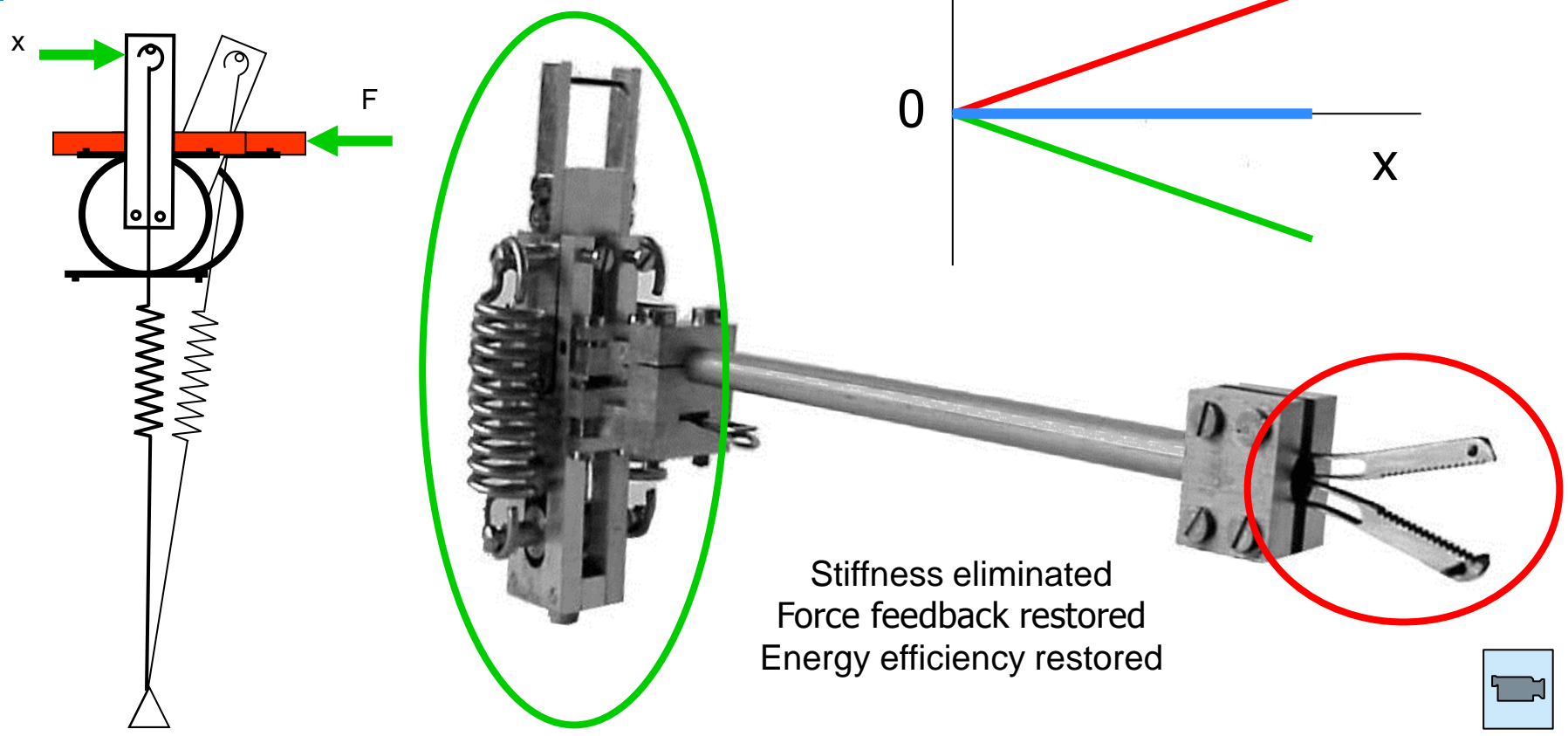
Hooke's law: $\sigma = E\varepsilon$

Stiffness: $F = kx$ ➔ Zero stiffness

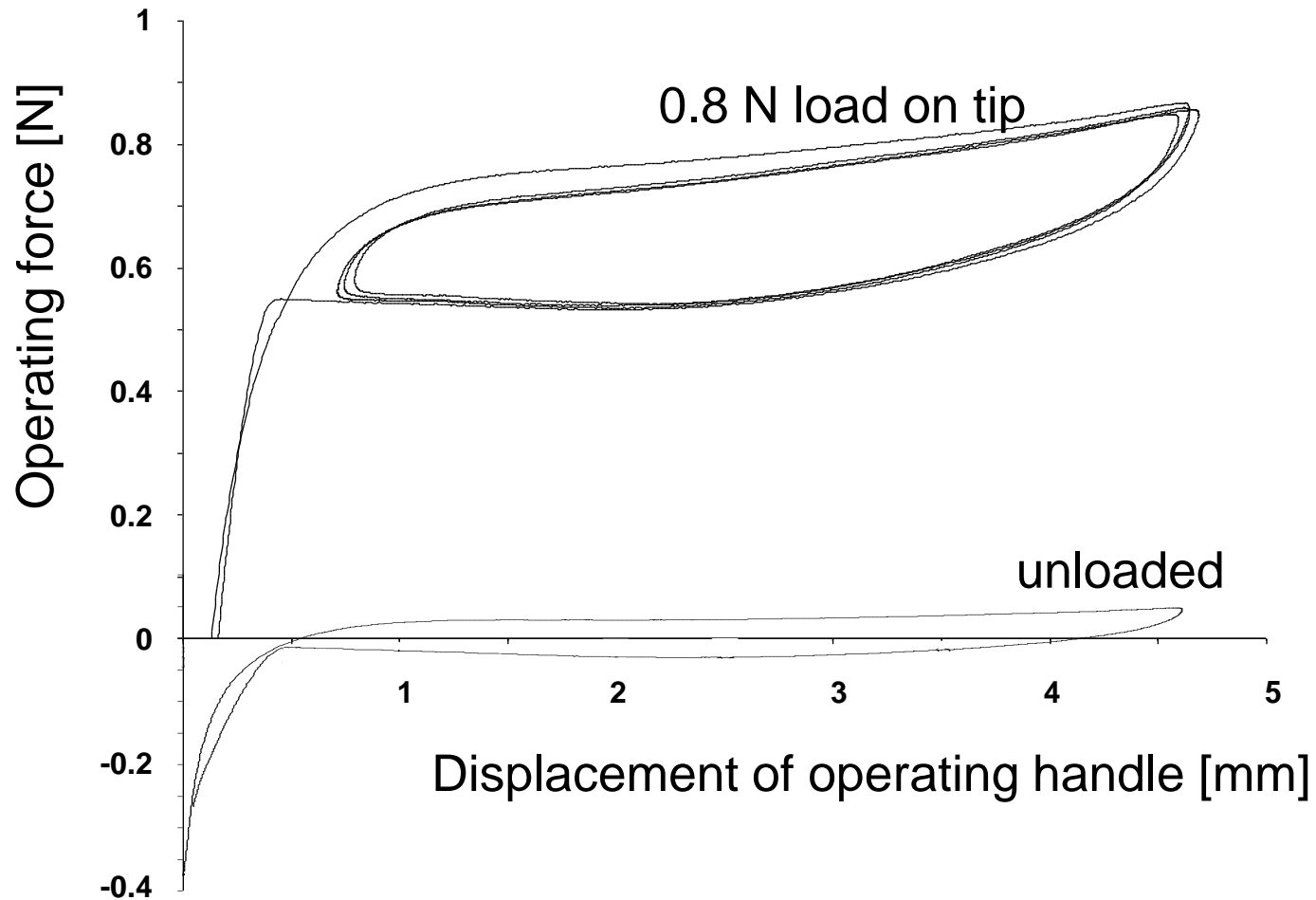
Challenges:

- Preload
- Tuning

Static Balancing of Compliant Mech.



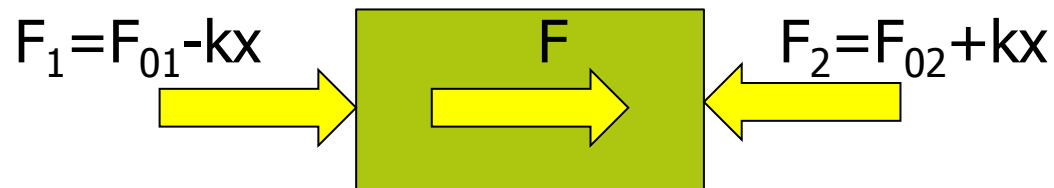
Rolling contact forceps



Does an opposite spring provide static balance?



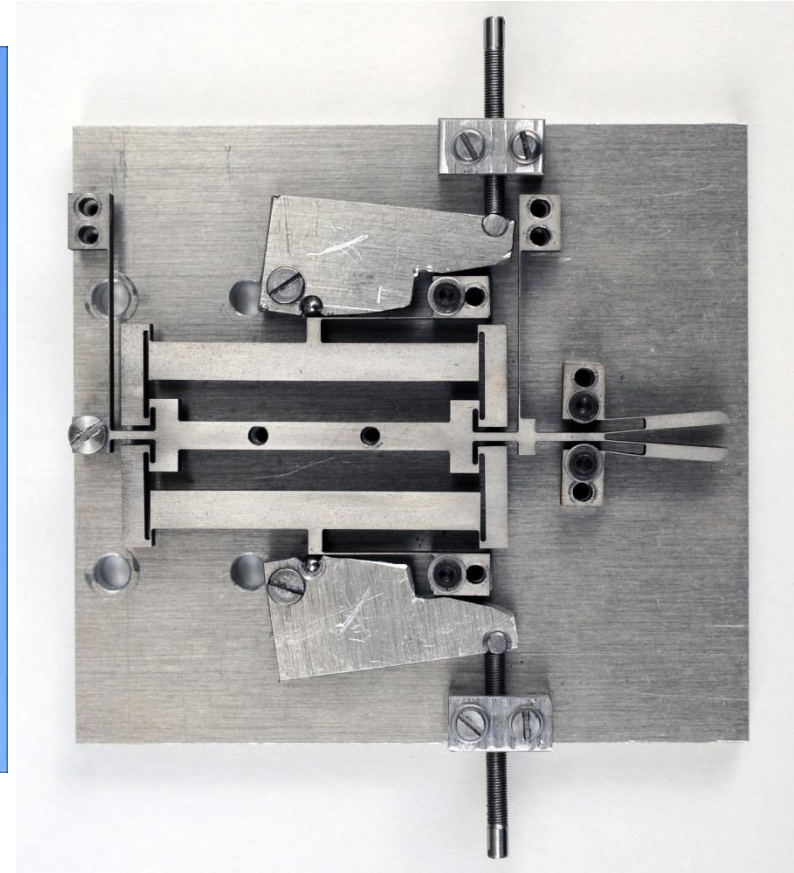
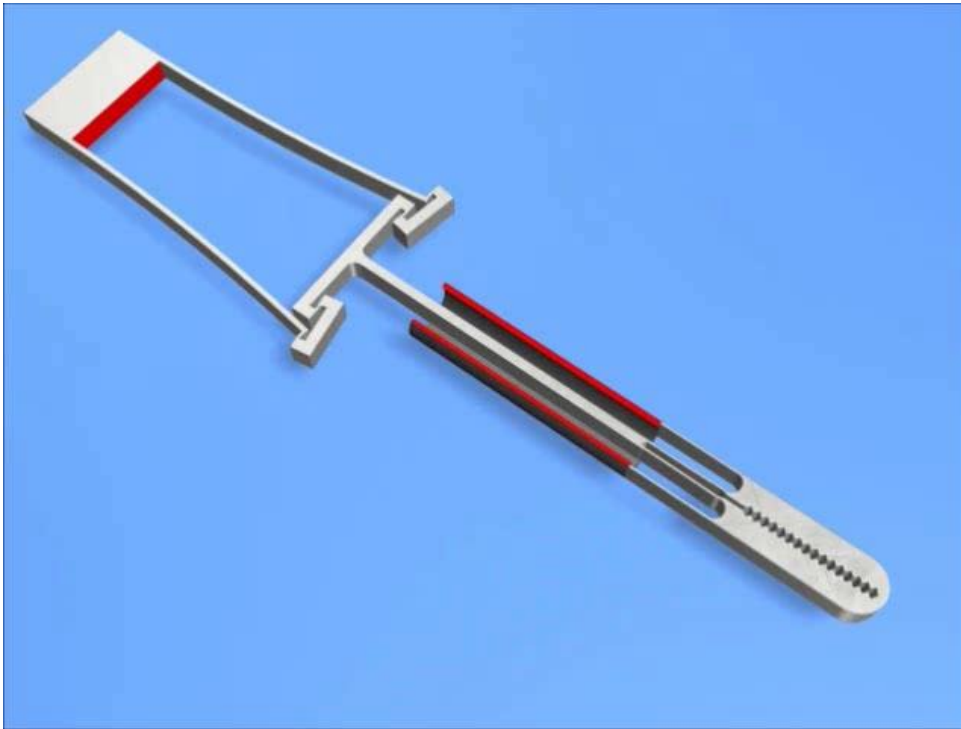
No they don't, in fact they double the stiffness



$$F + F_{01} - kx = F_{02} + kx$$

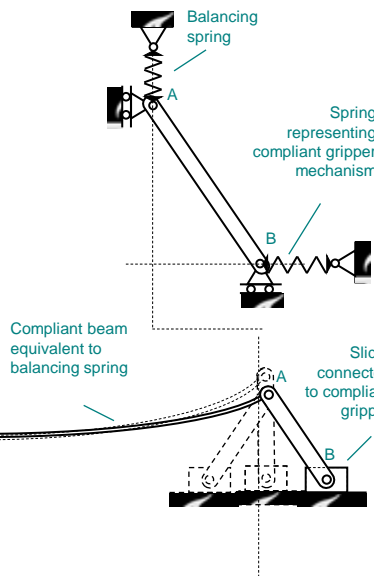
Preload drops out, $F = 2kx$, so stiffness doubled

Static Balancing of Compliant Mech.



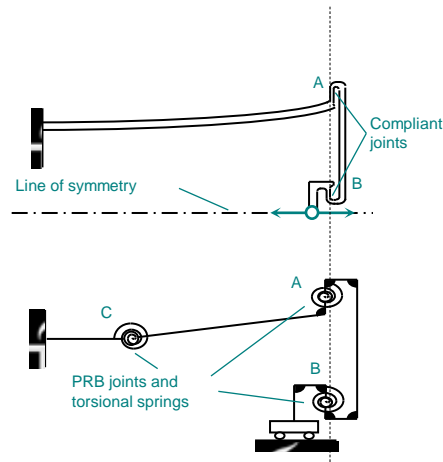
Design steps

1



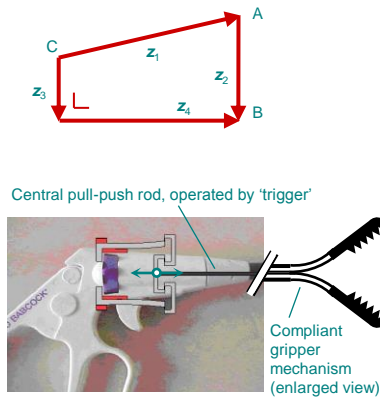
2

3



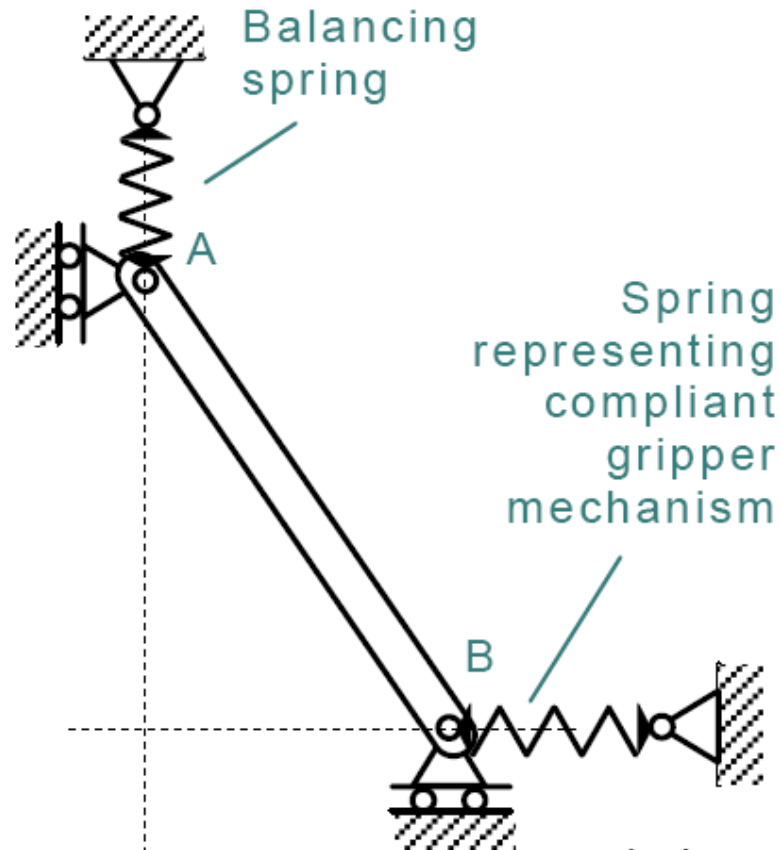
4

5-7

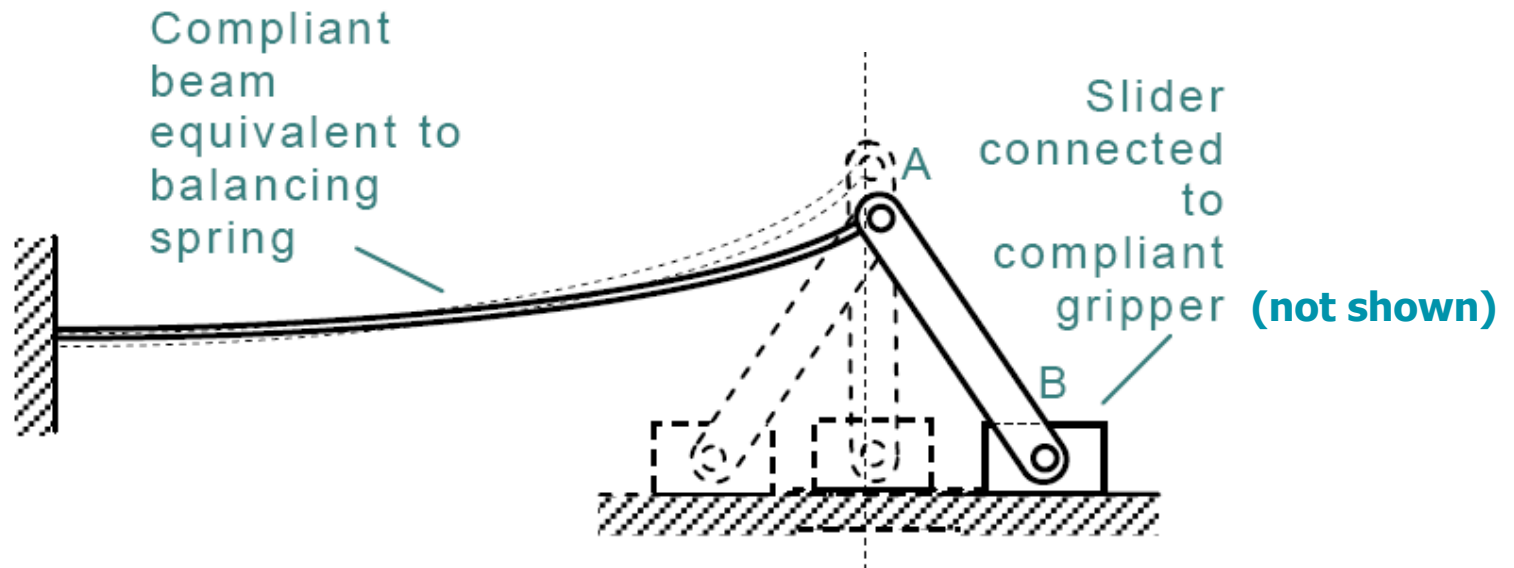


8-9

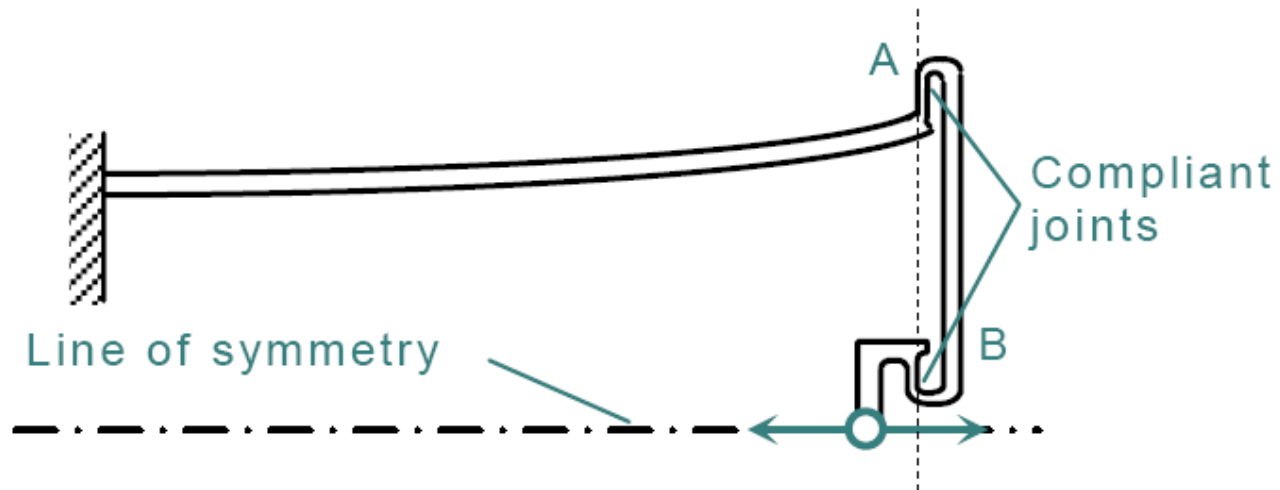
Step 1: Known rigid-link SB mech.



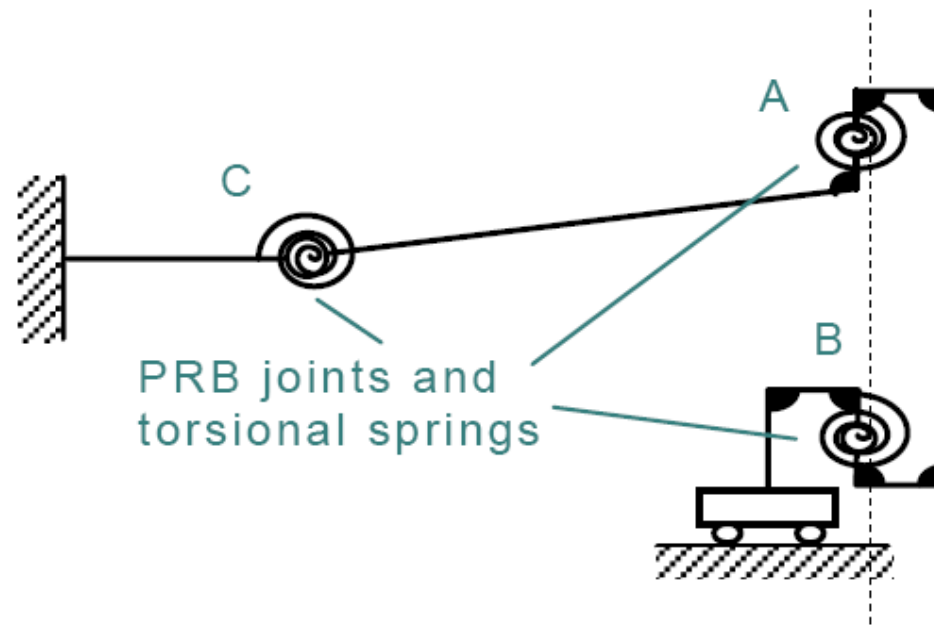
Step 2: Replace spring by CM



Step 3: Replace joints by CM

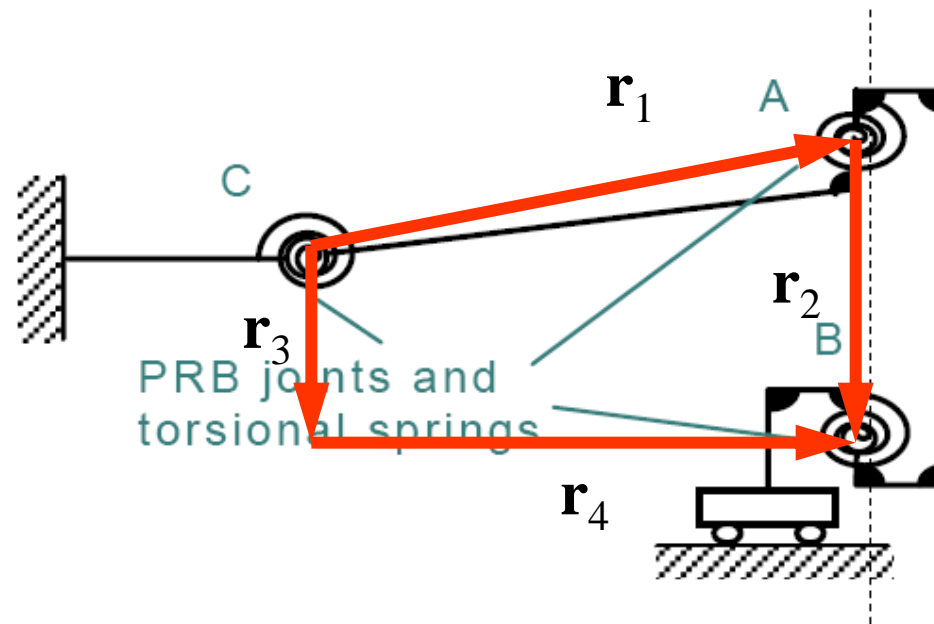


Step 4: PRB modeling



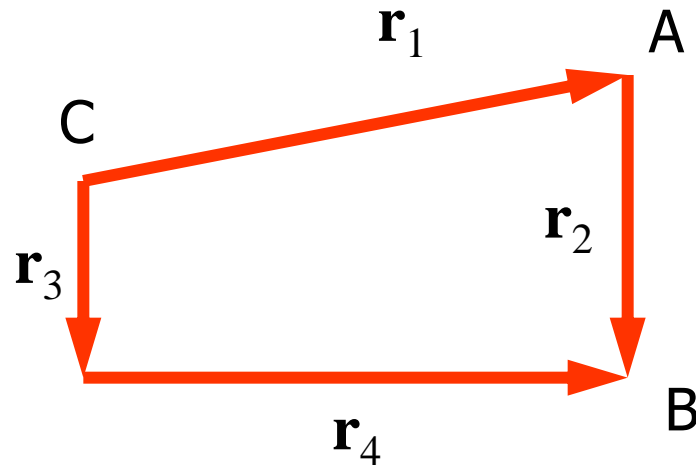
Few parameters, e.g. k_A , k_B , k_C , λ_C

Step 5: Kinematics, loop closure



Few parameters, e.g. k_A , k_B , k_C , λ_C

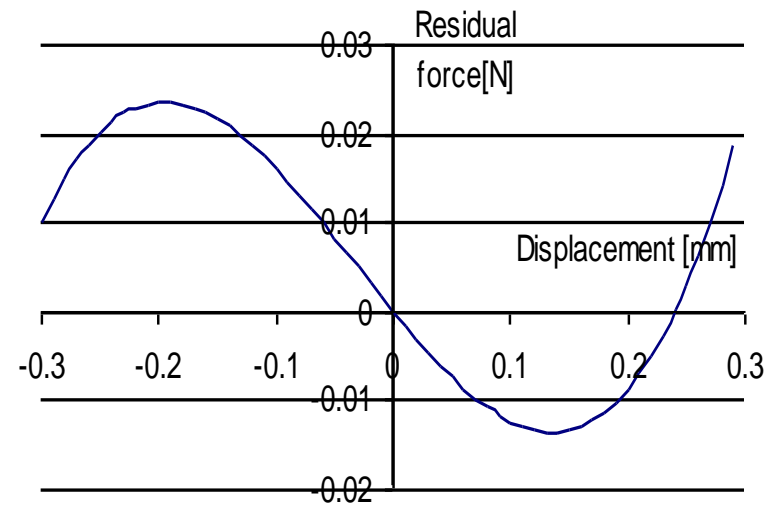
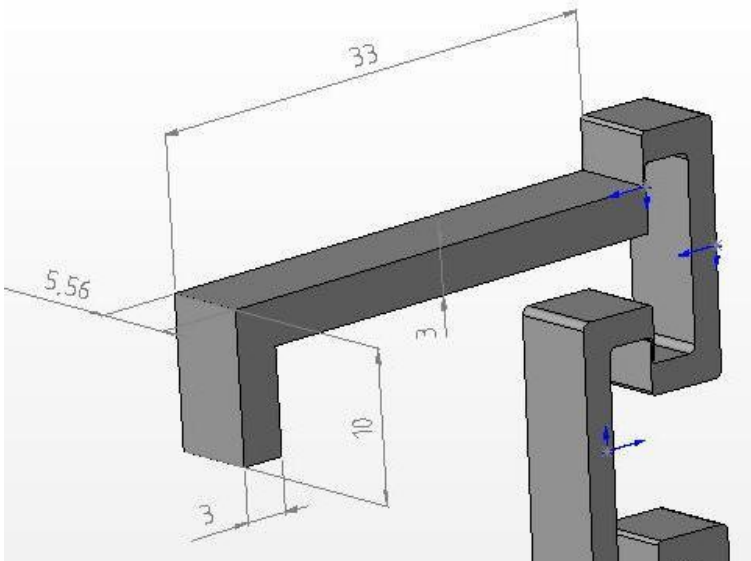
Step 5: Kinematics, loop closure⁺



$$\mathbf{r}_1 + \mathbf{r}_2 = \mathbf{r}_3 + \mathbf{r}_4$$

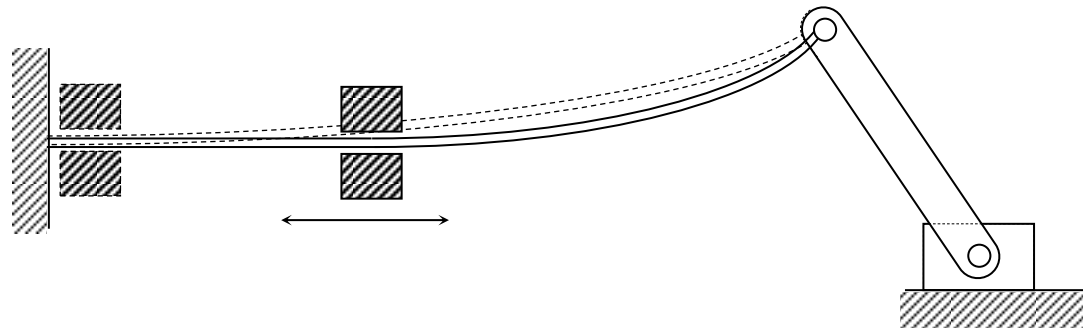
$$V_A + V_B + V_C + V_{\text{gripper}} = \textit{Constant}.$$

Step 6: Dimensioning the CM

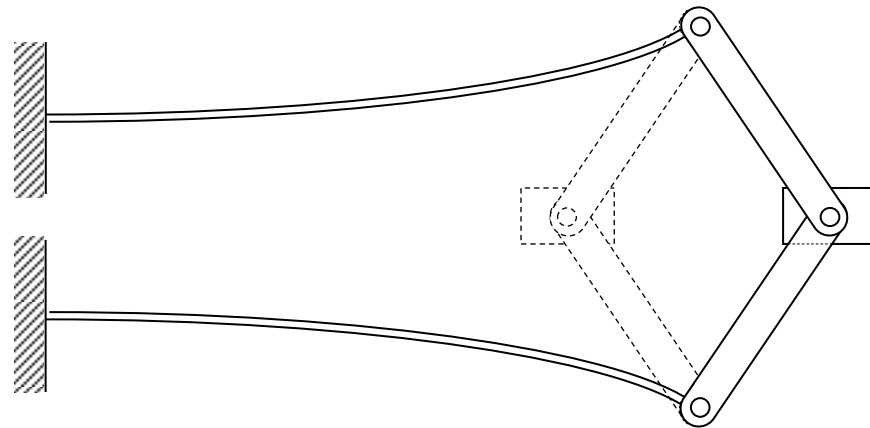


Step 7: Instrument design

Stiffness
adjustment

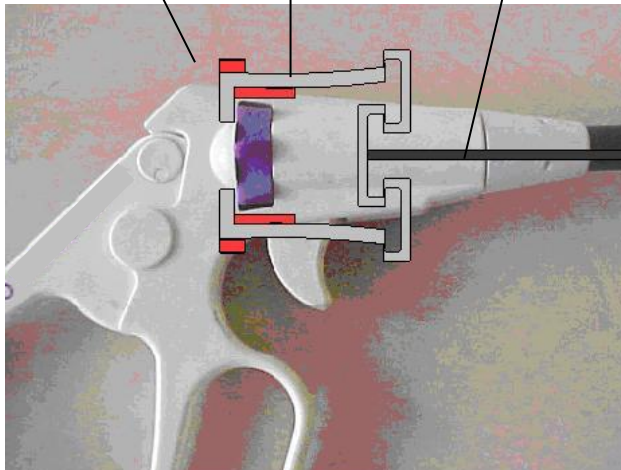


Symmetric
arrangement

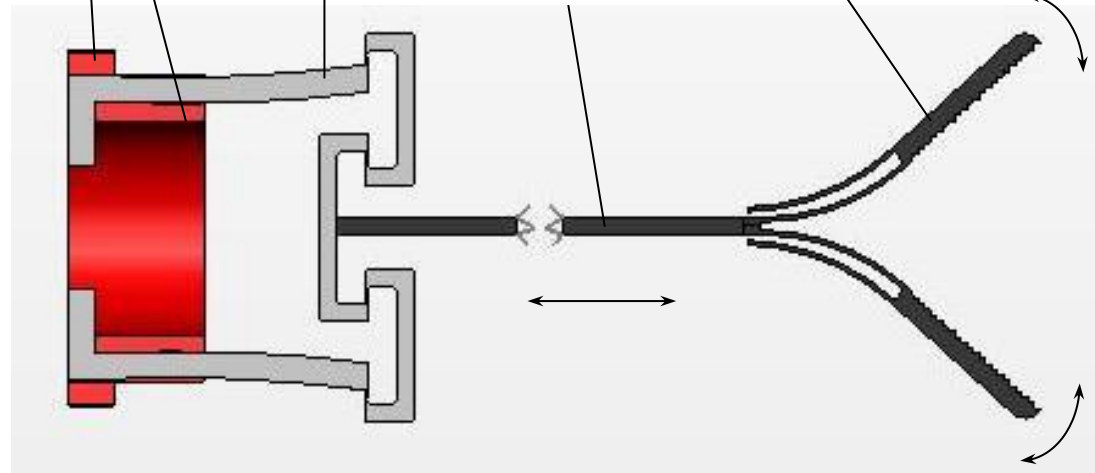


Step 8: Detailed design

Stiffness adjustment
Compensation mechanism
Rod between mechanism and gripper

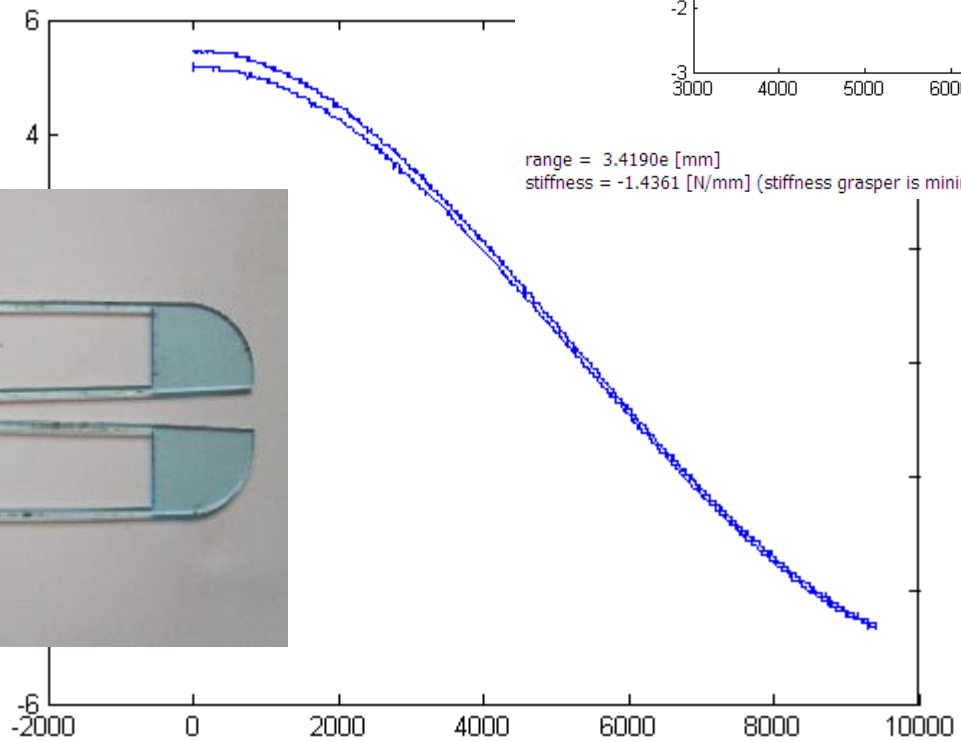


Stiffness adjustment
Compensation mechanism
Rod between mechanism and gripper
Gripper

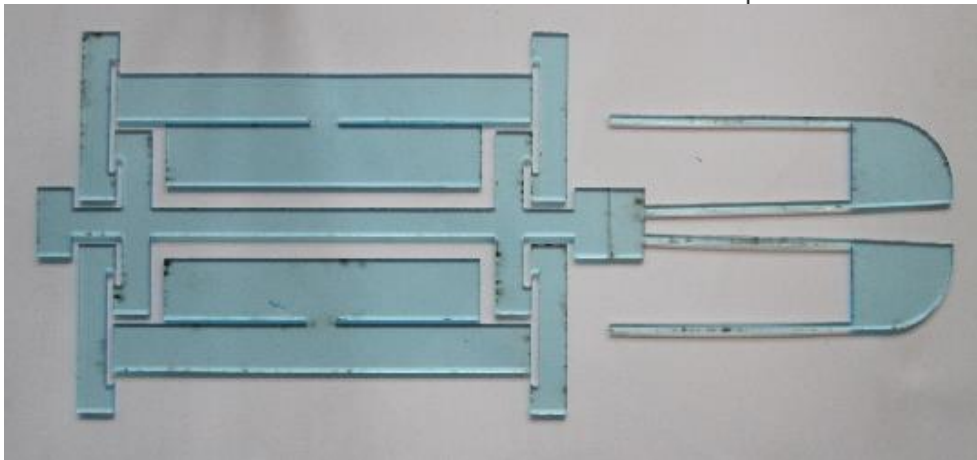
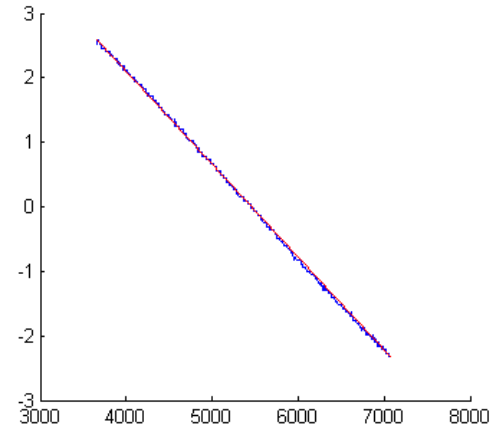


Step 9: prototyping

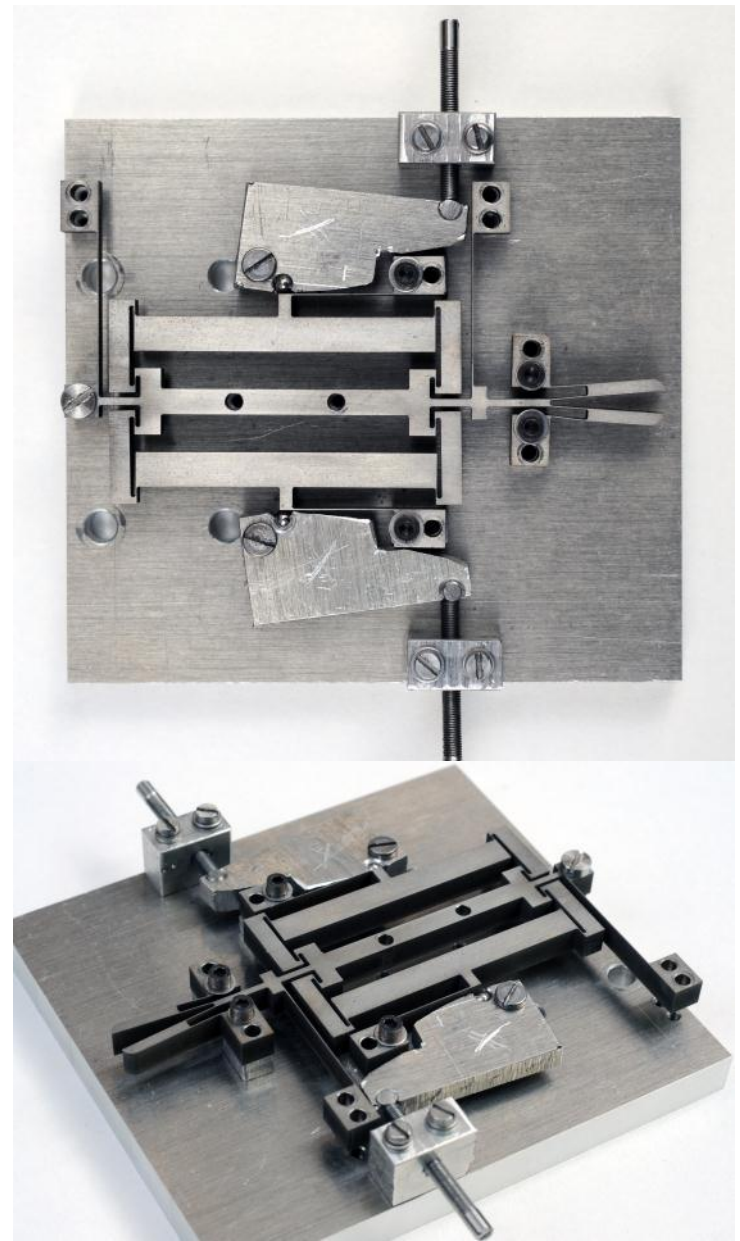
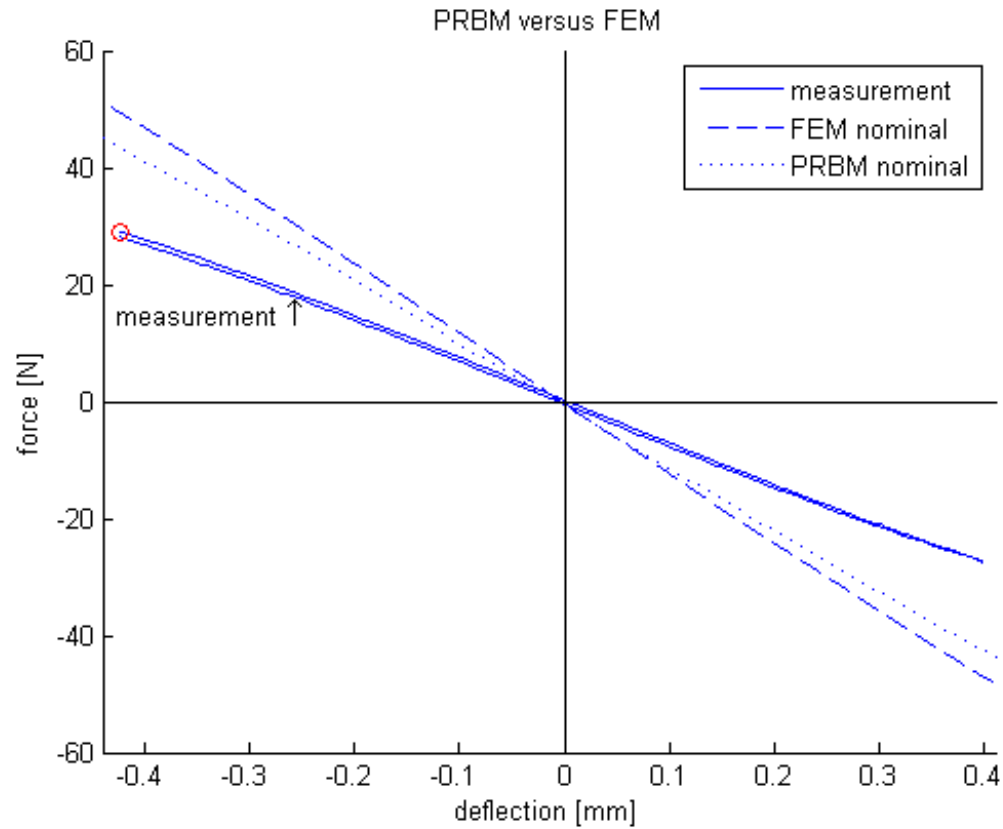
FULL RANGE (9.4 [mm], hysteresis plot)



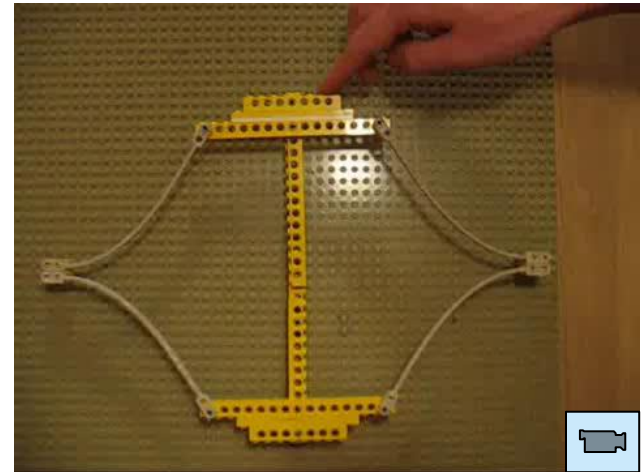
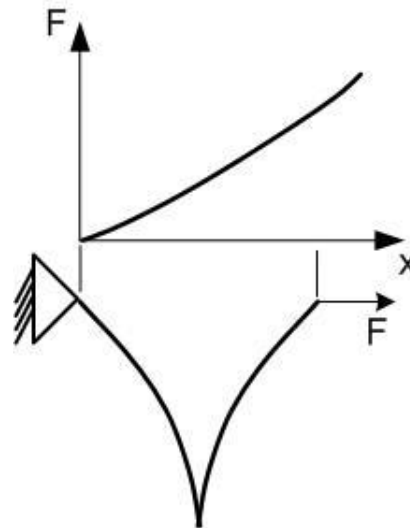
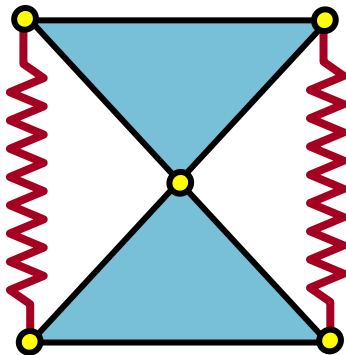
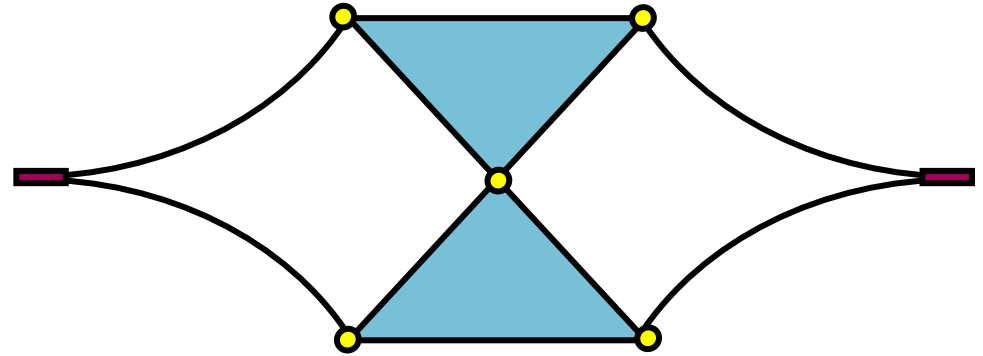
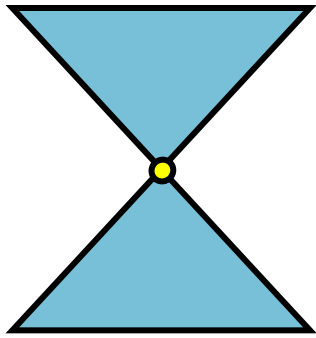
LINEAR RANGES



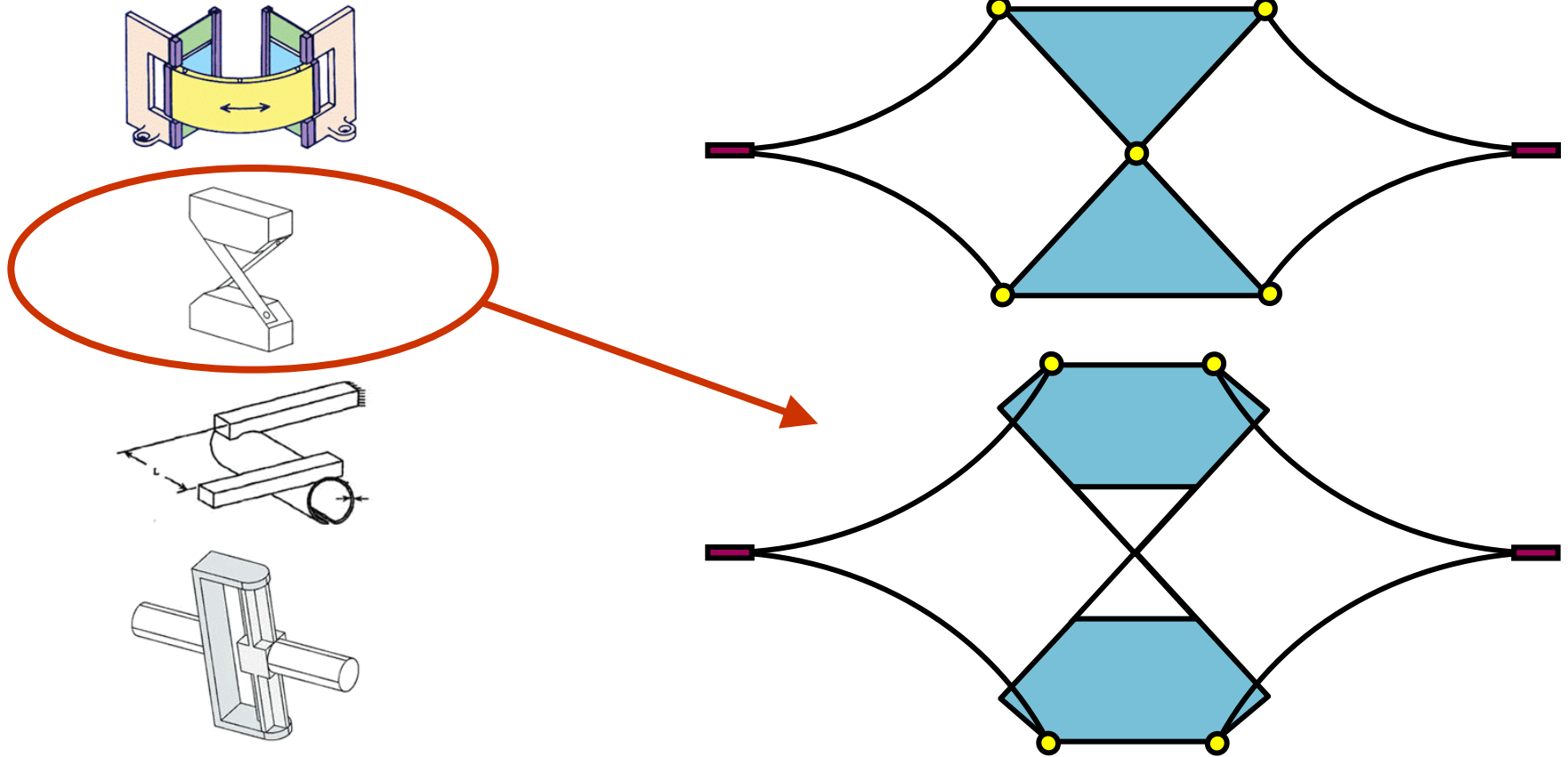
Step 9: prototyping



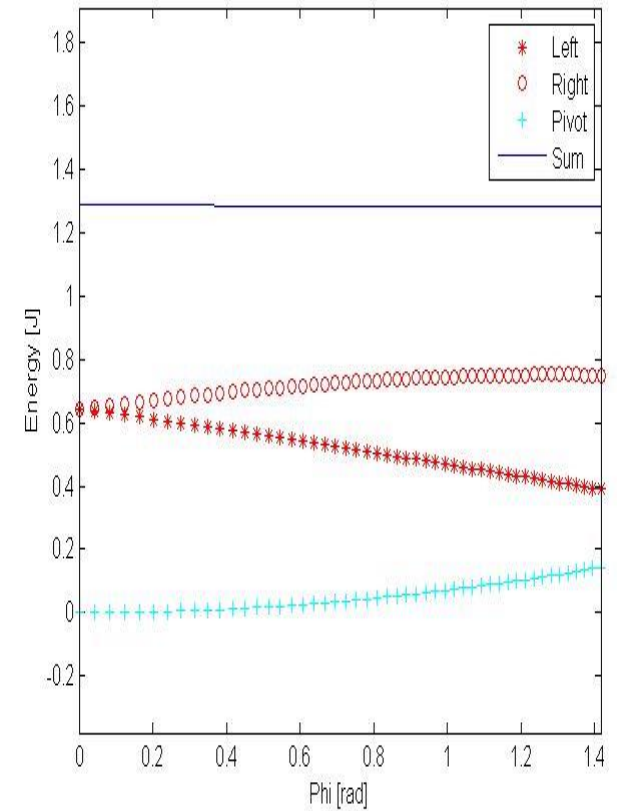
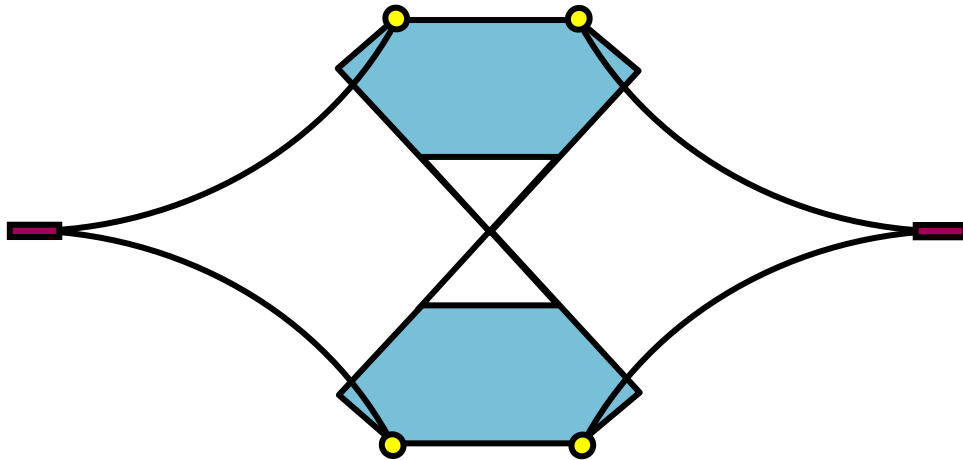
Zero stiffness joint



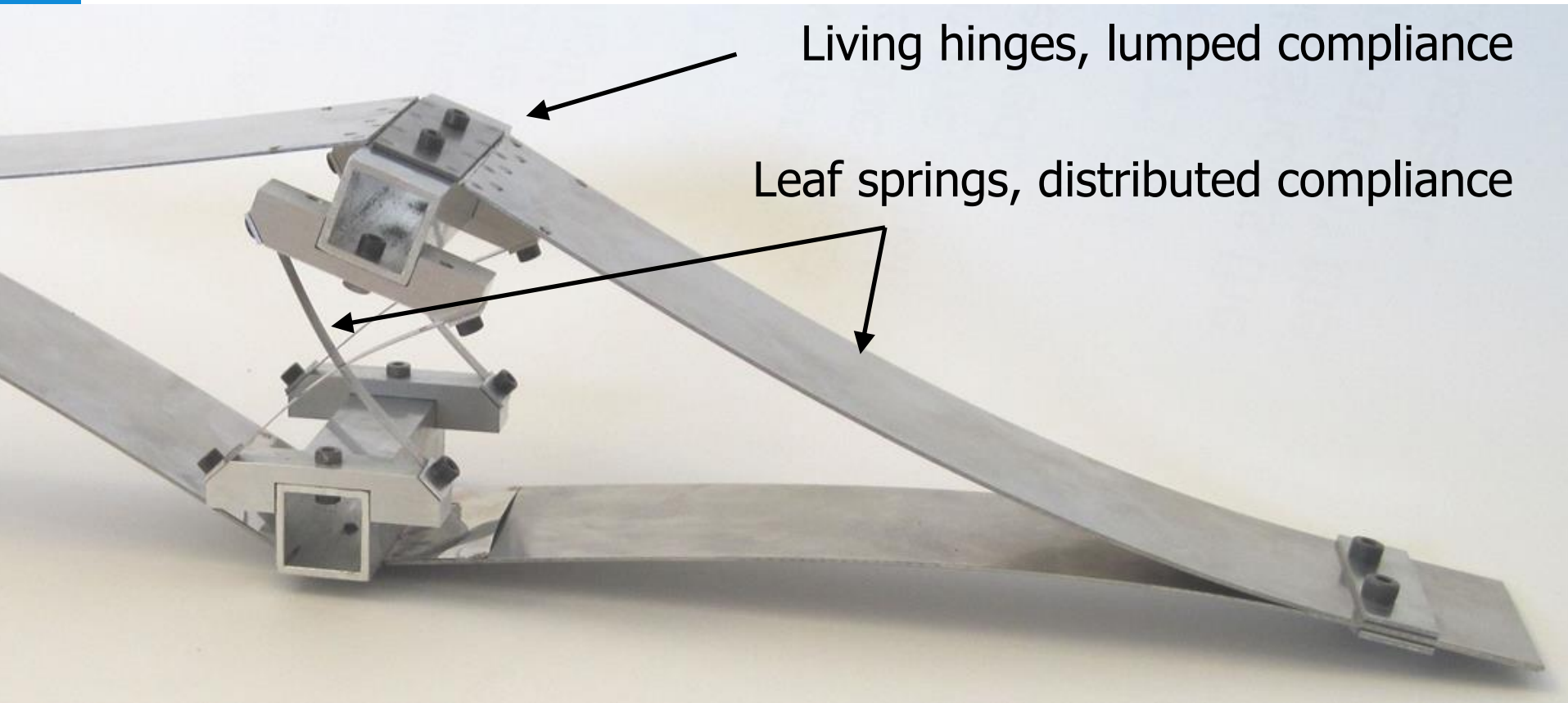
Zero stiffness joint



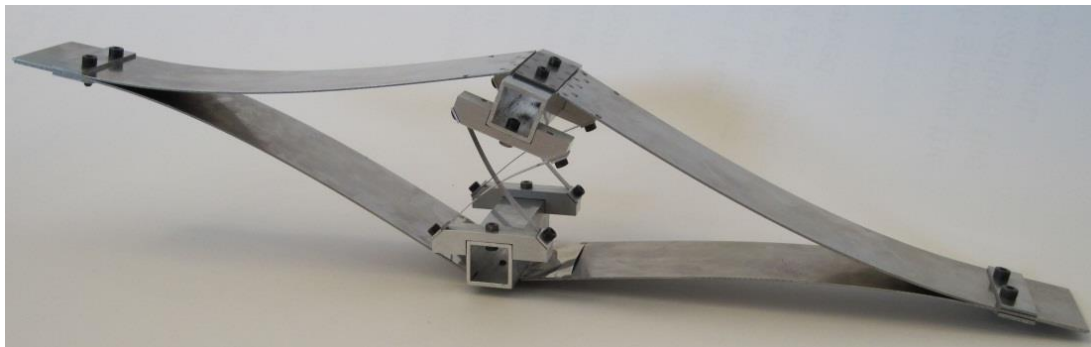
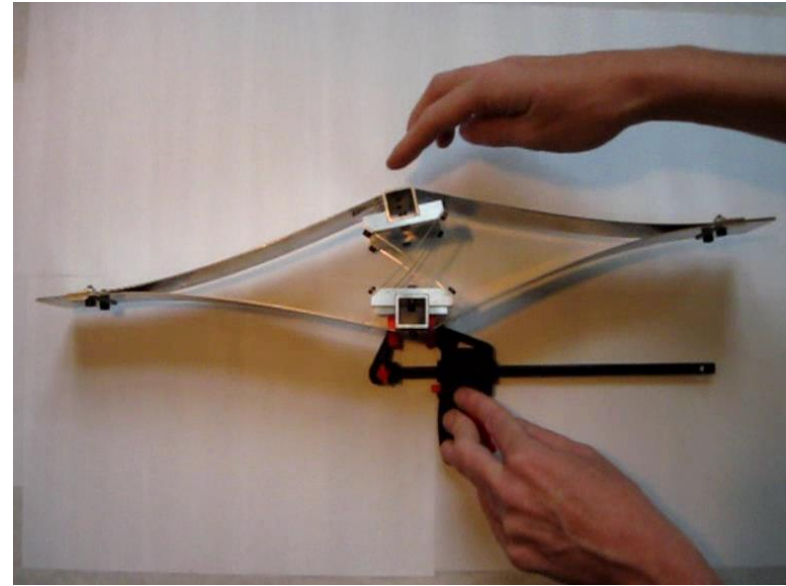
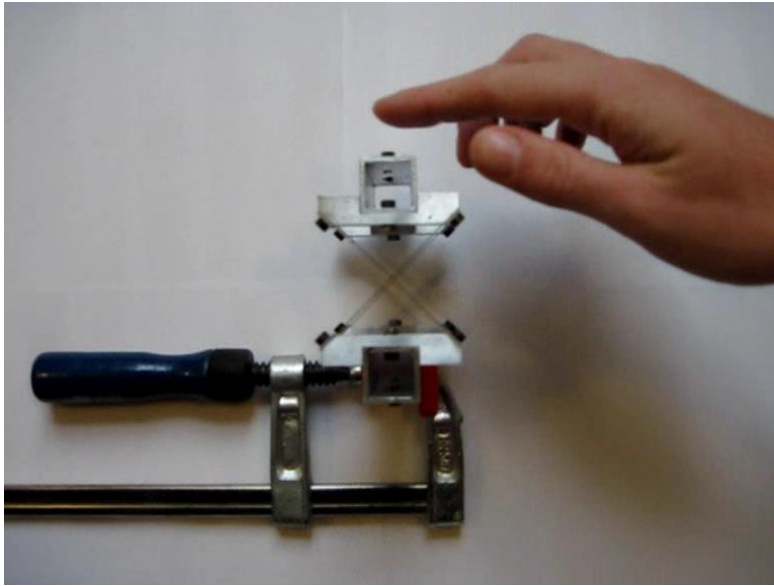
Zero stiffness joint



Zero stiffness joint

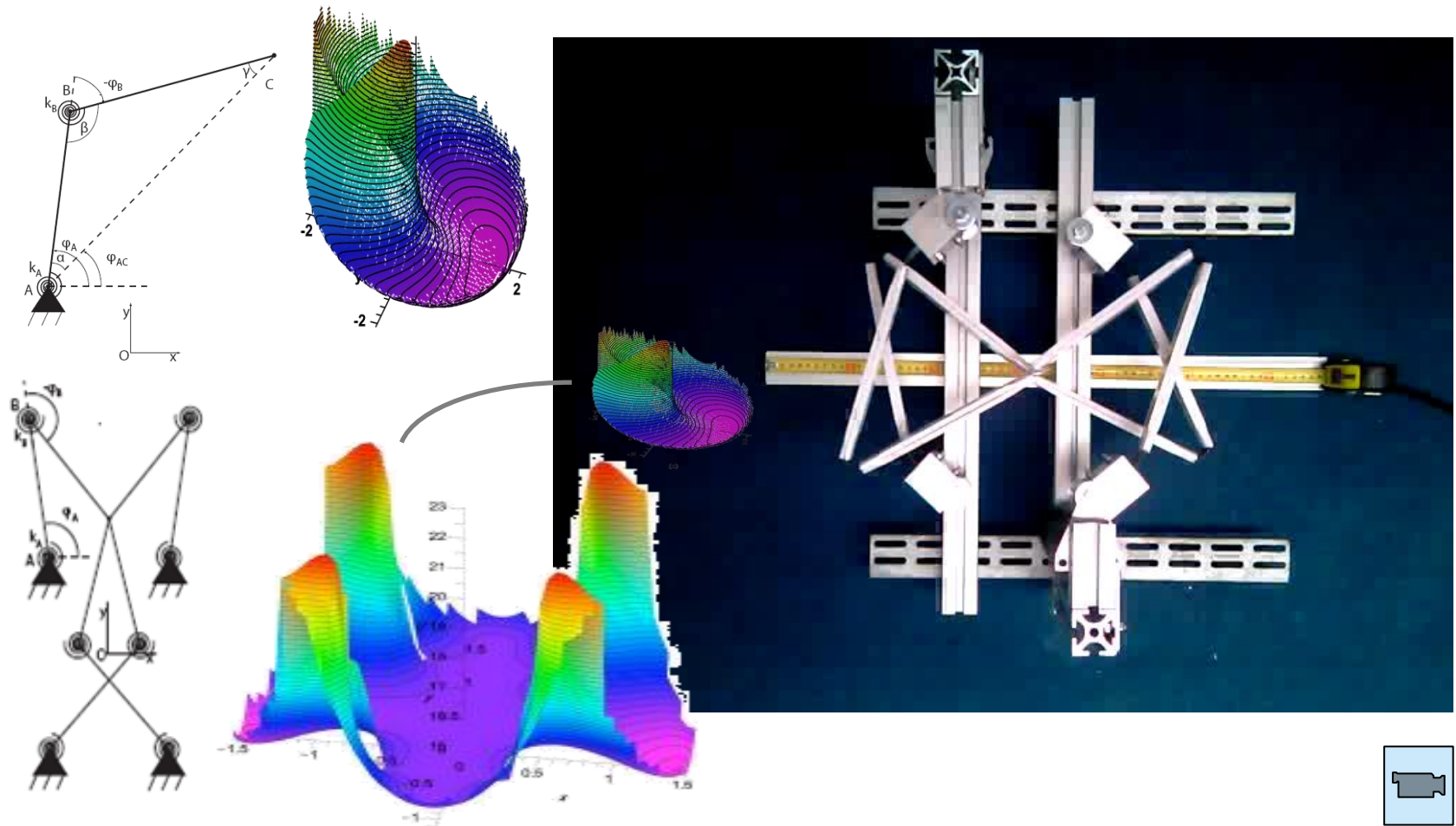


(Near) zero stiffness joint

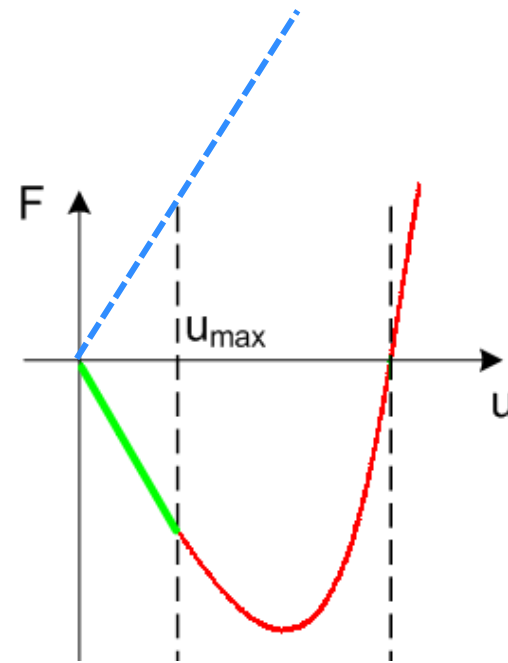
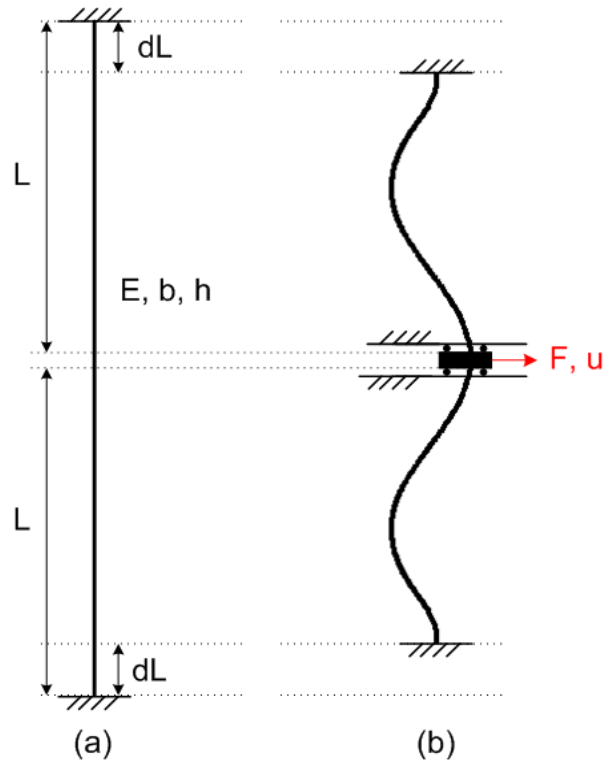


	Average moment reduction, $\varphi = 0$ -end trajectory [%]	Max moment reduction, $\varphi = 0$ -end trajectory [%]	End trajectory [rad]
PRBM	95	98	1.42
FEM	93	93	1.28
Experiment	70	63	0.58

Straight-line self-guiding SBCM



Static Balancing of Compliant Mech.



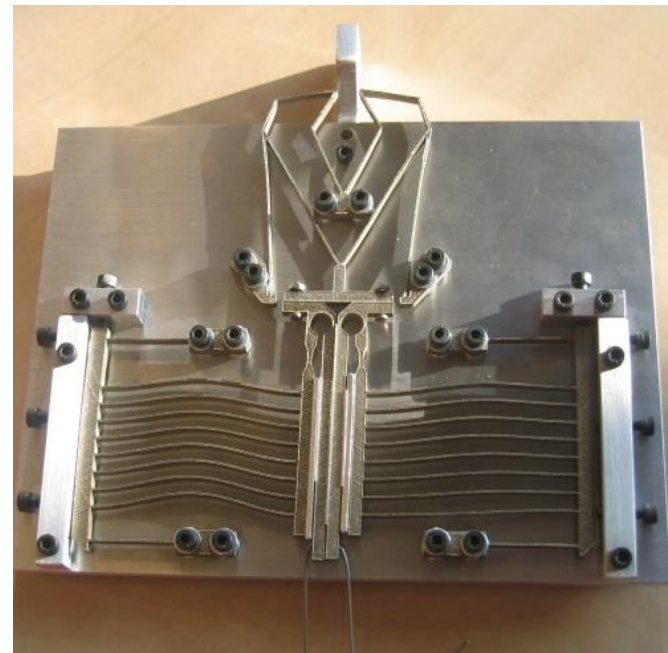
Static Balancing of Compliant Mech.



Statically balanced gripper

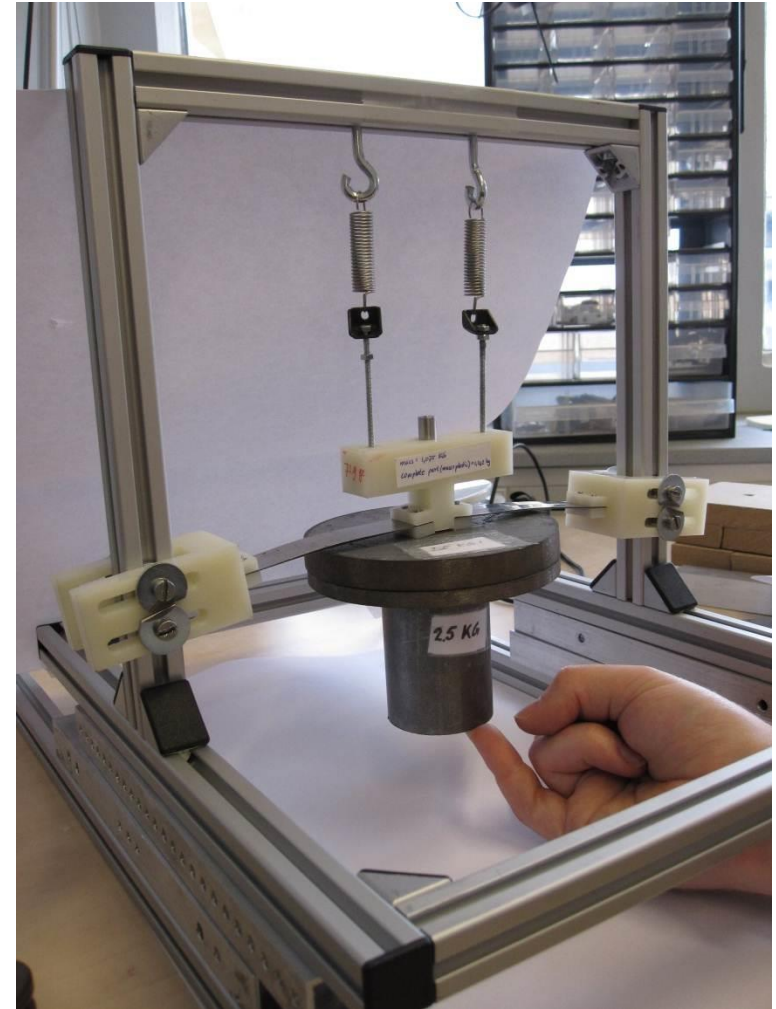
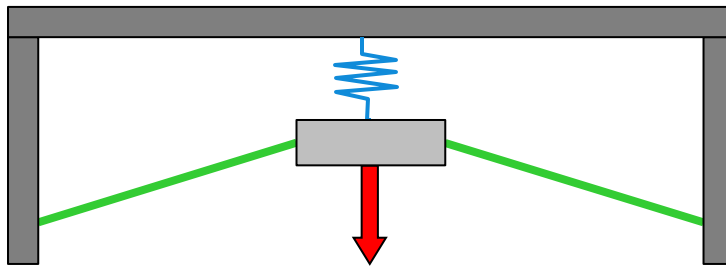
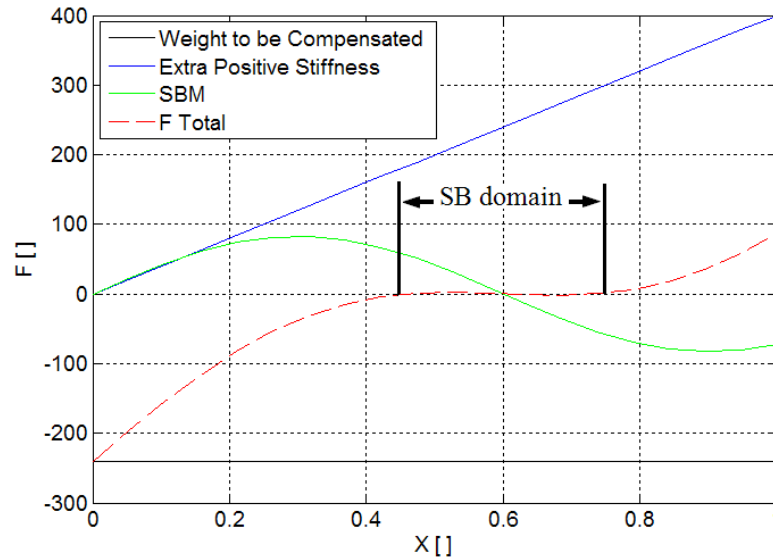
Karin Hoetmer, Charles Kim,
Geoffrey Woo, Just Herder
2009

Delft University of Technology
Bucknell University

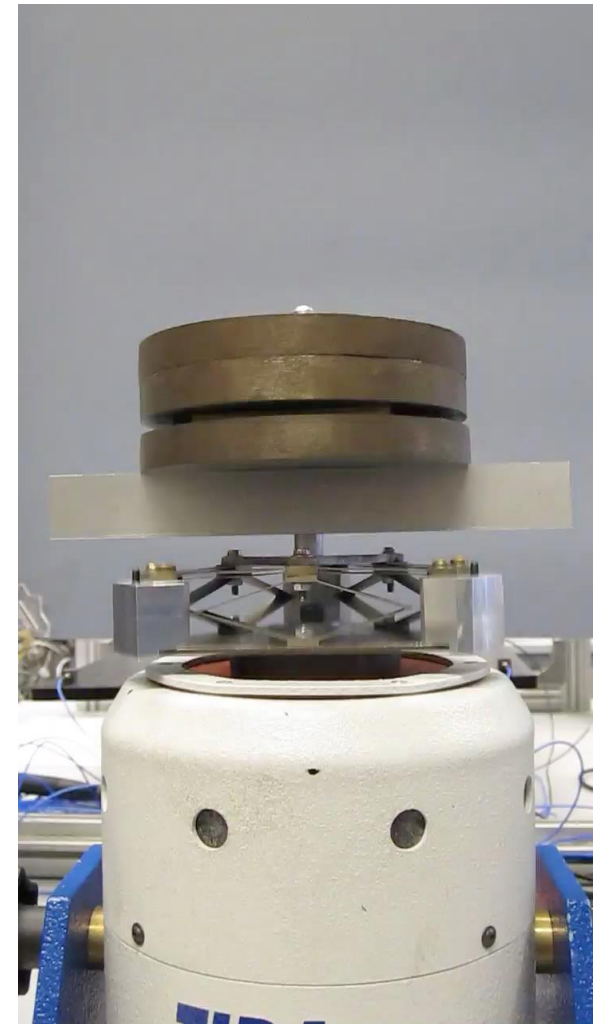
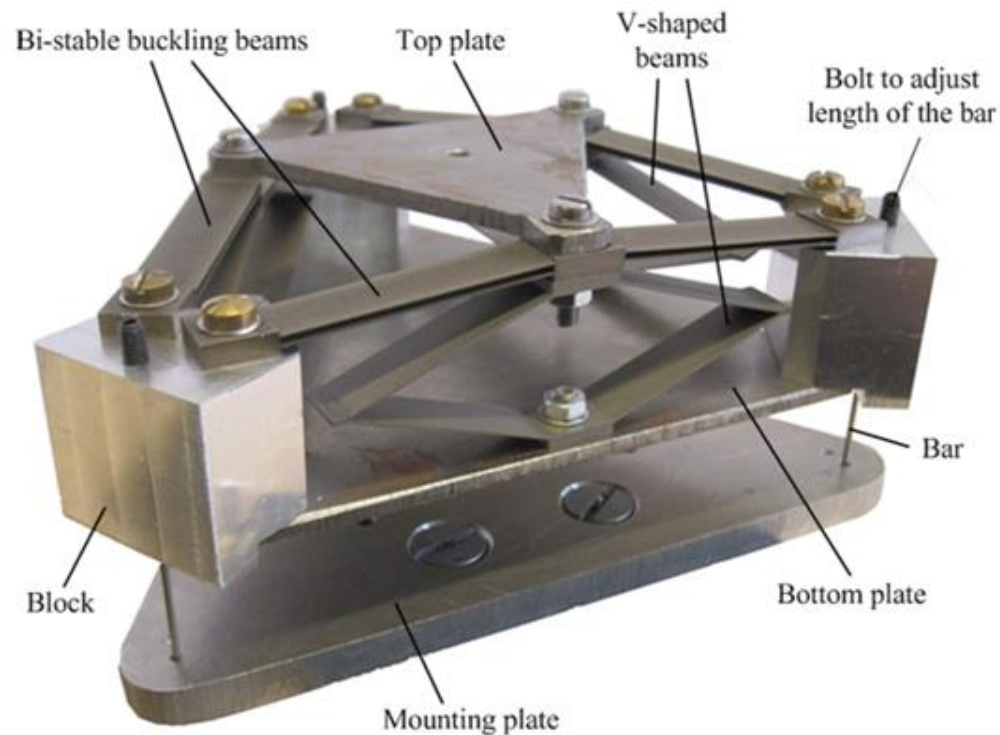


Constant force unit

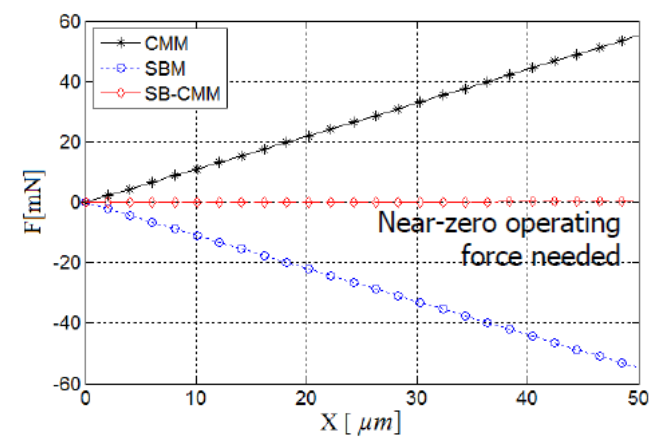
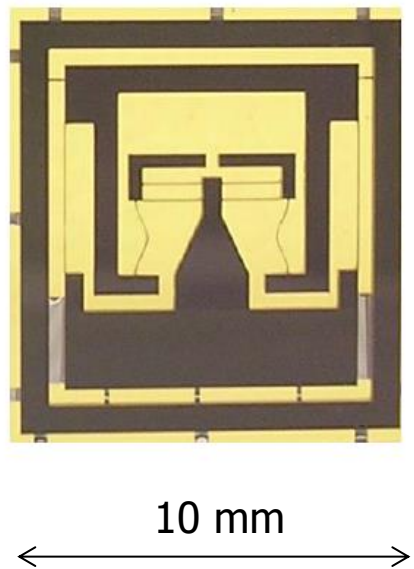
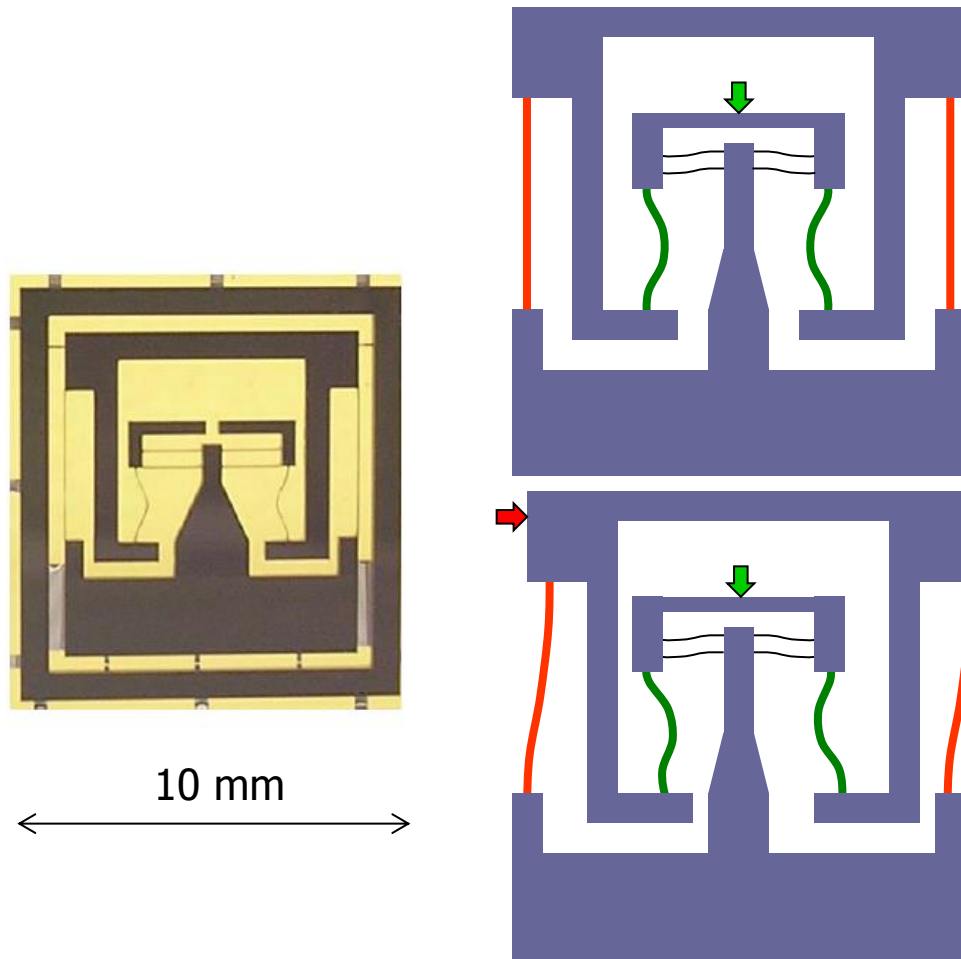
Force composition method



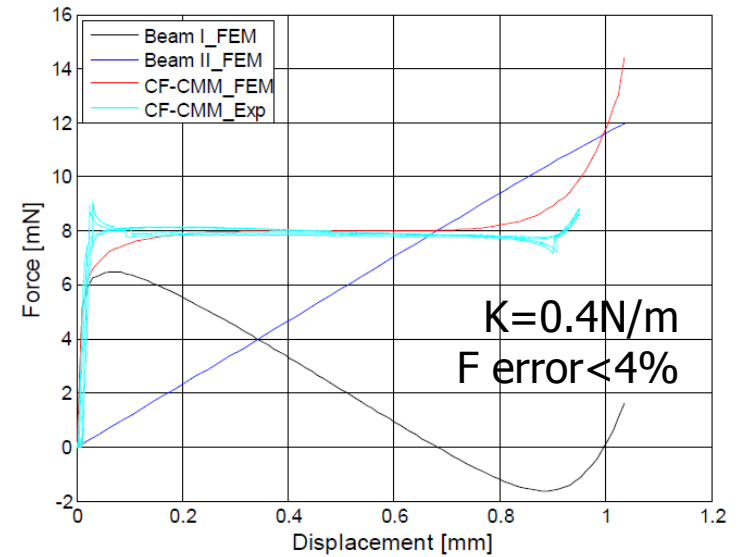
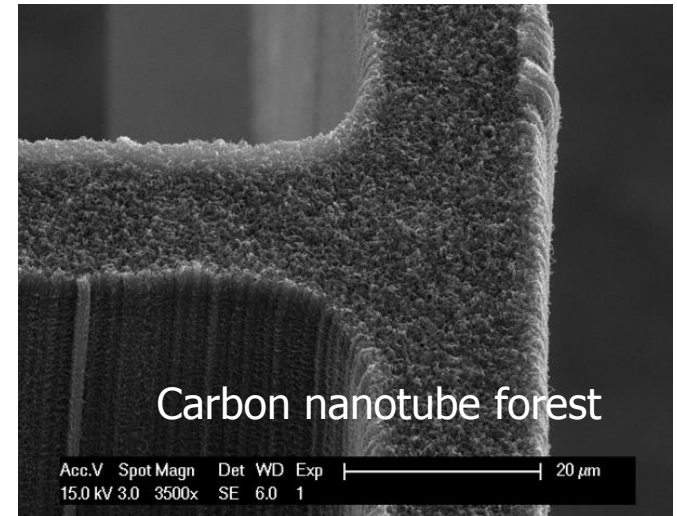
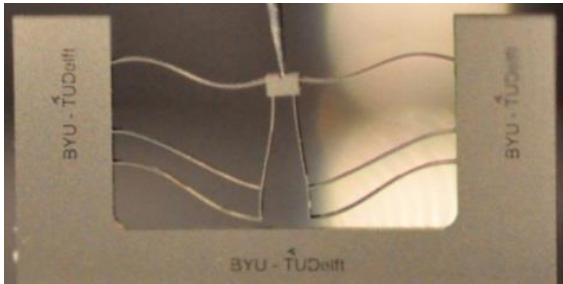
Vibration Isolator



Statically balanced micromechanisms



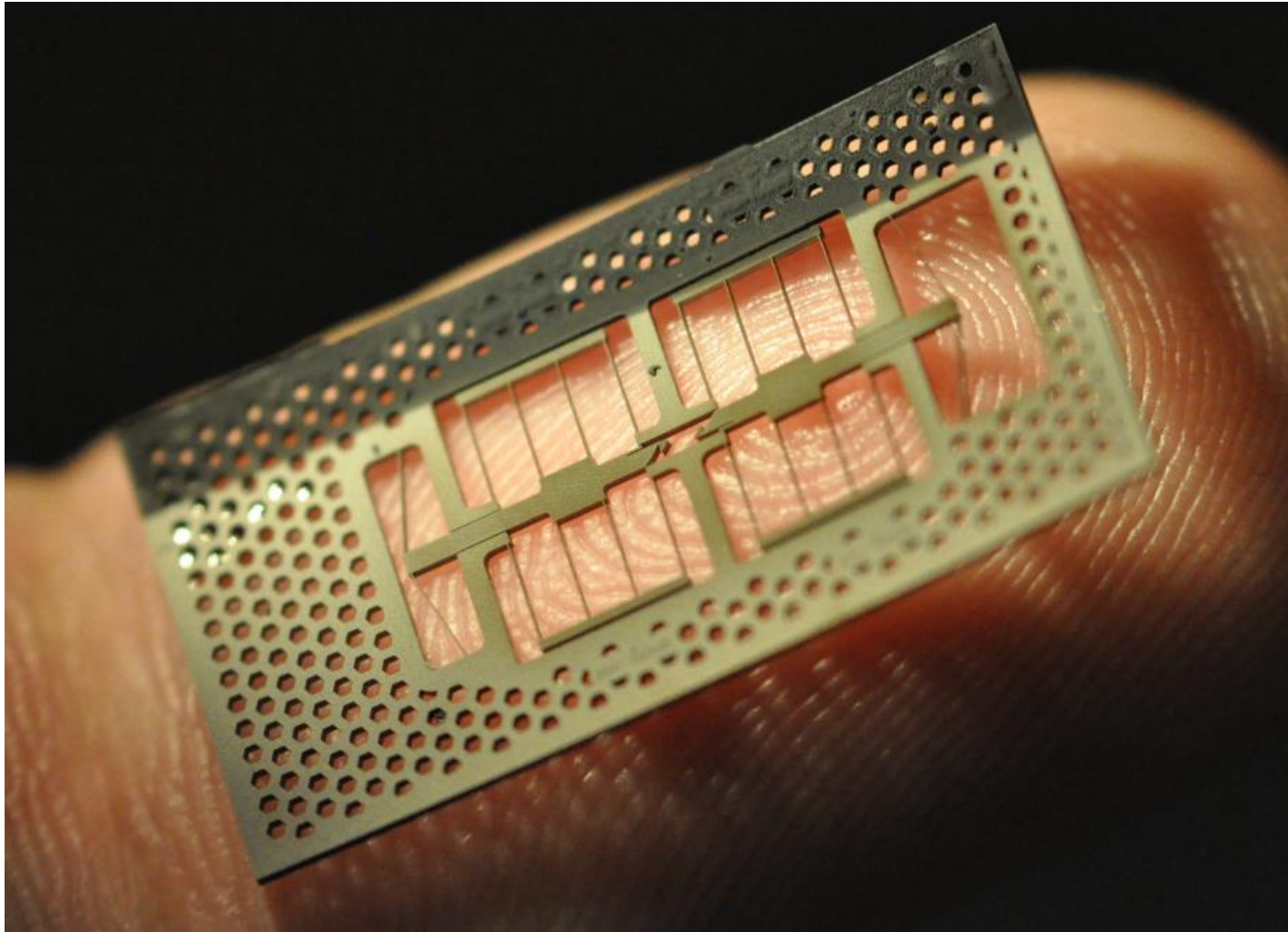
Constant force



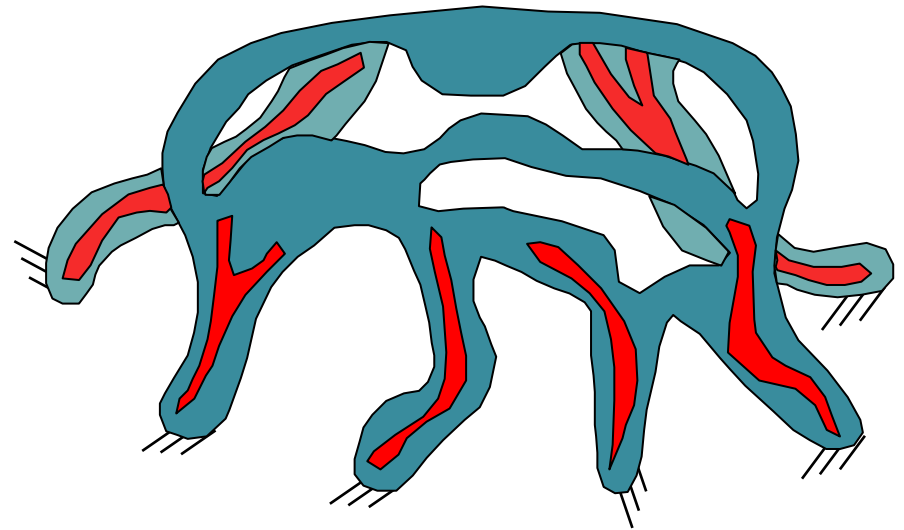
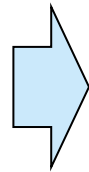
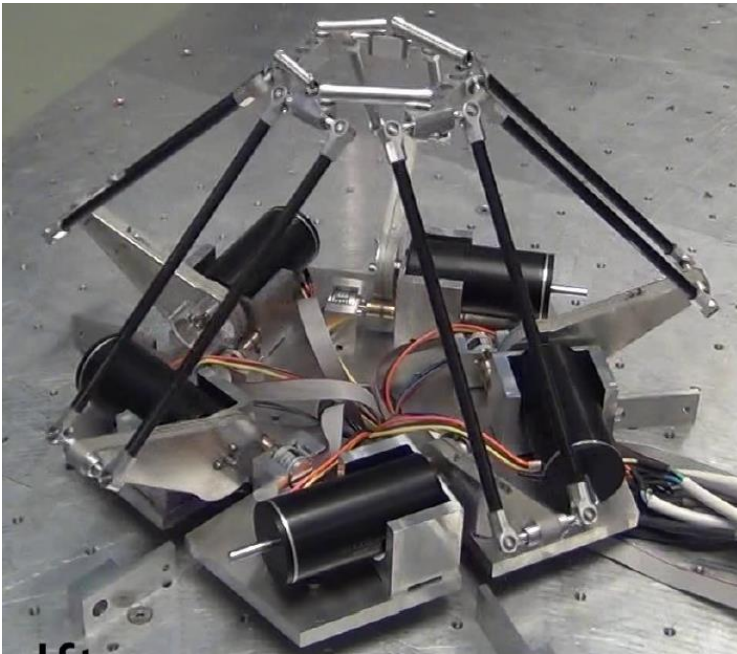
Preloading with ON/OFF switch



Towards zero force

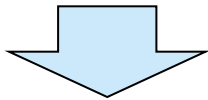


Next next generation

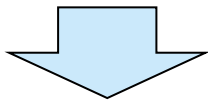


Research directions

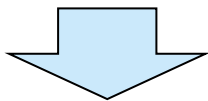
Large scale systems with special behavior



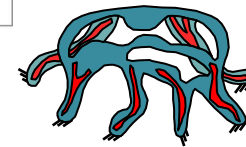
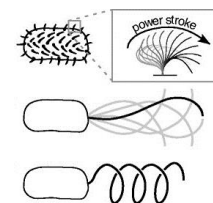
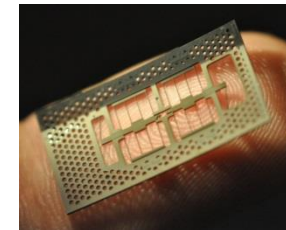
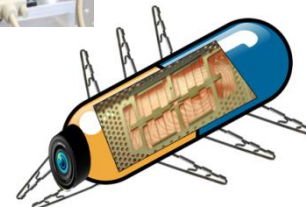
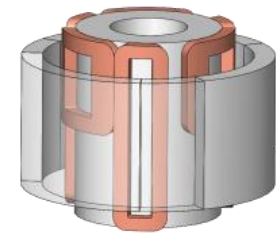
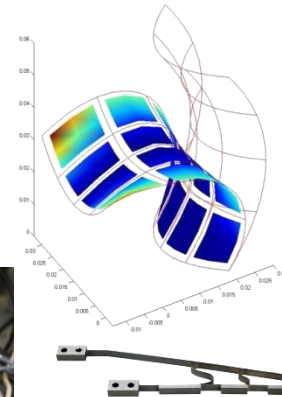
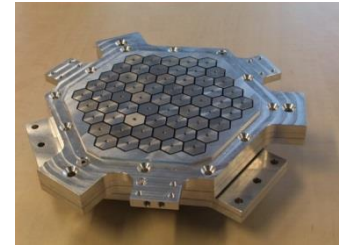
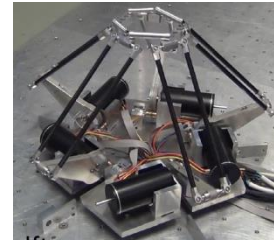
Large scale systems with micro/nano accuracy



Small scale systems with micro/nano features



Nano scale systems with nano accuracy





Strength and stiffness...
CM toolbox contains...
Stiffness is not...

Thank you!